Modeling AND SiMULATION OF MagNETIC TRANSMISSION LINES

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# List of Symbols

Symbol Definition Equation

Magnetic flux density vector (1.2)

Electric field intensity vector (1.2)

Force between magnetic poles (1.1)

Lorentz forcevector(1.2)

Electric charge (1.2)

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# Abstract

Magnetic Transmission Line [22-26] is the dual counterpart of Electric Transmission Line. Its theory encompasses a diverse range of applications including Transformers [17], Dynamic Machines [11] [20], Microwave Generators, Tuners, Couplers, Isolators, Power Dividers [58] etc. Intrinsically, Magnetic Transmission Line [22-26] is made from a non-conducting magnetic material, with a high permeability. It transmits Magnetic Flux as the effective Magnetic charge. Time varying magnetic flux results in a Magnetic Displacement Current inside the Transmission Line. This produces a gradient Magnetic Field; with Fields Lines that spread radially outwards. The magnetic displacement current and magnetic voltage due to this Magnetic Field is measured in Volts and Amperes respectively. Although, the operation of a Magnetic Transmission Line [22-26] does not involve electric charges, Magnetic Displacement Current produces an Electric Field with closed Field Lines encircling the Magnetic Transmission Line [22-26]. Together, the Electric and Magnetic Fields transmit Energy along the direction of propagation [55]. These relations were modeled using Maxwell’s Equations [55] and magnetic circuits to study the time and frequency domain behavior of Magnetic Transmission Lines [22-26]. Furthermore, Finite Difference Time Domain [68-69] [64] Electromagnetic Field Simulations [39] were carried out in MEEP [52] Simulator for anisotropic, inhomogeneous, non-linear Magnetic Transmission Lines [40] [65] [43] [22-26] [8].

The Magnetic Transmission Line [22-26] model is valuable for the design of Magnetic Elements like Inductors, Transformers and Filters [17] [20]. The conventional design of Magnetic Elements is an iterative procedure. There is no shortage of empirical formulas for estimating Magnetic Losses in Magnetic Cores [35-36] [20]. The literature derived formulas are specific for the particular Magnetic core shape and size. The procedure involves many approximations like uniform field inside core. The design involves hit and trial methods. The element is designed for particular frequency. The Magnetic Transmission Line [22-26] model can be extended to design accurate models for such magnetic elements [20]. An example wideband transformer [67] [31] [29] [14] [17] is designed with multiple outputs and a large bandwidth. The electromagnetic effects were compared with the results of the transmission line model.

# Acknowledgements

# 

# Introduction to Solid State Magnetism

The first chapter is dedicated to a brief review of the nature of Magnetic materials and the transmission of magnetic information using magnetic dipoles. Section 1.1. presents a summary of Magnetic Dipoles and Bulk Magnetization. Section 1.2. discusses the AC properties and losses of magnetic materials [35-36] [20]. Section 1.3. presents a literature review of Magnetic Transmission Lines [22-26] with major emphasis on the recent research on Giant Magnetoresistance [66], Magnetic Capacitance [74] [73], Magnetic Memory [41], Spintronic and Nanomagnetic Logic Devices [63] [42] [38] [34] [5] [15] [19] [30].

Magnetic Transmission Lines [22-26] are designed to transmit electromagnetic energy using strong magnetic fields. They are made of magnetic materials having very high magnetic permeability and a strong affinity for magnetic flux. When an external magnetic field is applied, magnetic dipoles react to align with it. This large scale cooperation enhances the Magnetic Flux Density inside the magnetic material. When the applied field is varied, the changing Magnetic Flux Density transmits the magnetic information across the magnetic material [13]. This phenomenon is called Magnetic Transmission [22-26].

It is important to note that charge transport is not involved in magnetic communication. Isolated Magnetic charges do not exist and magnetic conduction current can never flow in a Magnetic Transmission Line [22-26]. Magnetic Transmission is only possible through the alignment of magnetic dipoles in response to a stimulating Magnetomotive Force. This is termed as Magnetic Displacement Current.

Magnetic Transmission does not involve the flow of Electric charges either. Magnetic materials are very poor electric conductors; hence electric currents cannot transmit information across a Magnetic Transmission Line [22-26]. Changing Magnetic Fields produce Electric Fields which are transmitted through electric displacement currents. This causes polarization of atoms in the dielectric [50] magnetic medium which transmits Electric information across the Magnetic Material. Together, the Electric and Magnetic Fields transmit Electromagnetic Energy along the direction of propagation [55].

The following sections will elaborate on the subject of Magnetic Materials. A brief account on the losses [35-36] [20] in Magnetic Transmission Lines [22-26] will be given as well.

## Nature of Magnetic Materials

The basic building blocks of magnetic materials are fictitious magnetic monopoles which can be considered as magnetic charge carriers. In nature, magnetic monopoles always exist in pairs called magnetic dipoles. A monopole can have either positive or negative charge which is responsible for the magnetic field around it. The force between monopoles is proportional to the strength of the poles (q) and inversely proportional to the square of distance (r) between them:

Dipoles result from the microscopic bound currents due to the electrons circulating around the nucleus. The effect of each tiny magnet is similar to the effect of a current flowing in a loop. The identification of the North and South poles is dictated by the Flemming’s right hand rule.

Whenever a moving charge q is placed in an electromagnetic field, it experiences a force called Lorentz Force [55]. The direction of the force represents the direction of least pressure in the electromagnetic field. Lorentz Force depends on the velocity of the charge and the strength of the electric and magnetic fields:

If an orbiting electron is placed in a magnetic field, the net Ampere force on the current loop is:

The Force will produce a Torque which will rotate the tiny magnet in the direction of applied field resulting in the transmission of magnetic information. The Torque can be represented in terms of the magnetic dipole moment normal to the current loop:



Figure : Magnetic Transmission through transfer of Torque

The magnetic dipole moment of an orbiting/spinning electron is related to the g-factors for the spin and orbital angular momentum, the spin angular momentum operator and the orbital angular momentum operator [6] [15]:

.0023, .

The magnetic field of the orbiting electron interacts with its spin to produce intrinsic spin-orbit interaction [15]. Hence the moment attains discrete values depending on the spin and orbital quantum numbers [42]. The net magnetic moment of an atom or ion is the vector sum of the orbital and spin moments of all electrons in its outer shell. The energy levels of an electron split in a magnetic field due to Zeeman splitting and Heisenberg exchange interaction [15] [6]:

(1.6)

(1.7)

where is the exchange constant between state i and j.

Two dipoles attract each other if unlike poles are close to each other. On the other hand, two dipoles repel each other if like poles are closer. Inside an unmagnetized material, the magnetic dipoles are optimally oriented hence the net torque is zero. Only a few orientations can result in a net zero torque on all the dipoles in a magnetic material. Dipoles tend to align parallel to neighboring dipoles due to positive exchange interactions so that the lowest energy state can be achieved.



Figure : A minimum energy state configurations achieved by cooperation of neighboring domains

Atoms contain orbitals with discrete levels of energy for accommodating electrons. Electrons try to occupy the lowest energy orbitals first to minimize the energy of the system. An electron with clockwise spin can pair with an electron having anticlockwise spin. Hence, the clockwise spin cancels the effect of anticlockwise spin and no magnetic moment results [15].

An external magnetic field can cause a mechanical torque on a magnetic dipole. The moment tries to turn the dipole in the direction that decreases the overall energy of the system. Only unpaired spins contribute to the net magnetic moment. The resulting spin and orbital moments add up to produce a net Magnetization Vector Field M inside the magnetic material [15]. This field is proportional to the magnetic susceptibility of the material :

The Magnetic Field inside a magnetic material can be represented by a flow of magnet field lines [13]. The number of lines passing through a region of space is called Magnetic Flux (equivalent to magnetic charge). Magnetic Flux Density (B) represents the number of flux lines per unit area:

Iron, Nickel and Cobalt contain 4, 3 and 2 unpaired electrons per atom respectively [53]. Hence, the effect of Magnetization is very strong in these special elements and their alloys. Large scale cooperation between magnetic dipoles causes an enhanced Magnetic moment. Due to the high magnetic susceptibility, they are used in the production of Ferromagnetic and Ferrimagnetic materials [53].

The microscopic bound current responsible for producing magnetic dipoles cancels out inside a uniformly magnetized material. A net bound current flows at the surface of the material. If **M** is non-uniform, the bound current will be non-zero inside the material as well.

(1.10)

(1.11)

The parallel alignment of magnetic dipoles causes the creation of magnetic domains [27] to reduce the magnetic potential energy stored in the Magnetic Flux Lines. The Magnetic energy consists of the following:

1. Magnetostatic Energy: The energy needed to place the magnetic poles in a specific geometric configuration e.g. magnetized state [27] is proportional to the width of the magnetic strip (d) and the value of applied Magnetic Field Intensity (H). Transformers are made using insulated sheets of steel having high electrical resistance [17] [27]. Rolling of the sheets aligns the Magnetic domains and reduces the Magnetostatic Energy [27]. The expression for this energy is given below
2. Magneto-crystalline Anisotropy Energy: For crystalline structures with repeating atomic units, the domain magnetization tends to align along one direction more easily than other directions. Magneto-crystalline Anisotropy Energy is greater in hard direction as compared to the easy direction [27]. It depends on the anisotropy constants () and direction cosines () which project magnetization on the different axes e.g.
3. Magnetostrictive Energy: Magnetization and Demagnetization can cause changes in the dimensions of the magnetic materials [27]. These stresses are caused by shifting of atomic planes e.g. during alignment of domains. Magnetostrictive Energy represents the elastic potential energy stored in the constricted atomic configuration. It is proportional to the magnetostriction constant and applied stress .
4. Domain Wall Energy: A Domain wall is a region where the Magnetization in one domain gradually changes to the direction of a neighboring domain [27]. Domain Wall Energy represents the energy in the transition region. It is related to Anisotropy Constant (), Curie Point ( and atomic spacing (a).



Figure : Tansition of spin direction at a domain boundary

Naturally, the size and direction of magnetic domains [27] is chosen to minimize the overall magnetic energy of the system. If an unmagnetized material is placed in an external magnetic field, the domains may have to align in a hard direction for Magnetization of the material. Work will be done to align the domains in the special configuration so that the preferable domains grow in size while the unfavorable domains shrink. This will involve displacement of atomic planes and domain boundaries. Hence the overall stored magnetic energy of the system will increase during magnetization [27].

When a demagnetized material is placed in an increasing Magnetic Field, the domain walls will start reversible movements and rotations. The Magnetization will start to increase slowly as shown in the Figure below. This corresponds to the elastic phase with minimum magnetic susceptibility. Later on, the domain wall motions increase greatly. Large scale irreversible atomic plane displacements correspond to the partial magnetism phase in magnetization curve. During this phase, the material exhibits the highest magnetic susceptibility. Soon the majority of domains get aligned with the magnetic field. In the last phase, a large amount of energy is needed to rotate the remaining domain magnetization hence the material exhibits a saturating magnetic susceptibility. At high fields, the induction saturates at Bmax.



Figure 4: Effect of Applied Field on Magnetic domains

If the applied field of the saturated material is decreased, the magnetic domains start to reverse their direction [27]. Initially, the material exhibits a small magnetic susceptibility. This resistance results because the majority of domains are aligned in the easy direction. The favorable domains had shrunk during the magnetization. Work must be done to expand the favorable domain walls in the reverse direction. As a result, demagnetization does not follow the curve of the original magnetization. When the applied field is decreased further, the magnetic susceptibility of the material starts to increase as more domains start to align in the reverse direction [58].

The induction lags the applied field hence some remnant induction remains when applied field is reduced to zero. In order to demagnetize the material, some extra amount must be applied. This amount is called the coercive force. As the field keeps decreasing, the domains start aligning in the hard direction. Once all the domains have aligned, the material saturates in the reverse direction.

If the material is now magnetized again, the response will contain all the phases described earlier. The induced field will start to increase slowly, followed by a phase of large magnetic susceptibility and end by saturating.

Hysteresis [44-46] can also be experienced in a single domain particle as dictated by the Stoner-Wohlfarth model [58] [48]. In actual anisotropic materials, susceptibility is represented by a tensor [48]. When a ferromagnetic material is magnetized, the susceptibility follows the blue curve . In order to reduce its magnetization to zero, the applied field is decreased. The anisotropic behavior can explain the hysteresis in ferromagnetic materials.

The slope of the B-H curve is called permeability [58]. It is closely related to the magnetic susceptibility.

When the material is saturated, the magnetic susceptibility becomes zero. Hence the permeability reduces to . Besides Magnetic Field Intensity, permeability is strongly dependent on chemical composition, crystal structure, stress, temperature and time after magnetization [58].



Figure : Variation of Magnetic Susceptibility with applied Magnetic Field



Figure 6: Hysteresis Loop

According to the Curie Weiss Law [6], the susceptibility decreases rapidly when the temperature is increased beyond the Curie temperature , when the ferromagnet becomes a paramagnet.

According to the Landau mean-field theory for ferromagnetism [62] [6], the Magnetization is related to temperature by the relation:

The Spin wave Theory of Felix Bloch [15] [6] states that Magnons carry quantized energy and momentum at T > 0 K. Each Magnon has spin . Their exchange interactions are responsible for the delocalized spin transitions inside the ferromagnet which reduce the magnetization from the maximum value .

The Bloch relation for the Magnetization is given below.

The experimental results deviate from the theoretical formulas near the Curie Temperature. From experiments, it has been concluded that ferromagnetic materials have the following exponential relations for susceptibility and Magnetization near Curie temperature [15] [6]:

## AC Losses in Magnetic Materials

After the brief introduction of the hysteresis loop [48] in the last section, this section will explain the different mechanisms of AC losses [35-36] [20] in magnetic materials.

The cyclic magnetization of a Magnetic Material causes many energy losses [35-36] [58]. The atomic plane displacements and domain wall rotations cause mechanical losses in the material. Induced voltages cause circulating currents and electrical losses. At microwave frequencies, magnetic resonance and complex permeability [72] [70] [58] [35-36] [12] [16] can cause a significant increase in the losses [35-36]. The various loss mechanisms [20] are:

1. Hysteresis Losses: During the traversal of magnetization loop, energy is lost as heat during irreversible domain changes [58] [35-36] [48] [44-46]. The permeability changes with position, the applied field strength, time after demagnetization (disaccommodation), frequency and temperature [35-36] [58] [20] [44-46]. Fields inside Anisotropic media can be represented by a 33 permeability/ magnetic susceptibility tensor [58]:

This hysteresis loss [44-46] is equal to the area inside the DC hysteresis loop [48] [58]:

Hysteresis loss increases with the applied field strength and frequency [58] [20] [44-46]. The empirical formula for Hysteresis Loss Density [48] is:

1. Eddy Current Losses: Ferromagnetic materials are semiconductors with resistivity () ranging from 0.1Ωm to greater than 1MΩm. The associated permittivity causes dielectric losses [50] [35-36]. Whenever a changing electromagnetic field is impressed induced voltages are developed in the material [55]. These generate circulating eddy currents in the material and produce Ohmic losses [20] [35-36] [58].

These losses can be reduced by using thin laminated magnetic films or magnetic grains for manufacturing. The Eddy current losses [35-36] [20] depend on the frequency (f), the applied field intensity () and the resistivity () or conductivity () [58]. The empirical formula for Eddy Current Loss Density is:



Figure : Dielectric circuit model for Ferromagnetic material

The Eddy Current Losses [20] can be enhanced at high frequencies due to dimensional resonance [12] [13] [35-36]. If a dimension of the magnetic material is equal to a quarter multiple of the electromagnetic wavelength, a standing wave can develop inside it. Under this condition, the in-phase flux cancels the anti-phase flux so the observed permittivity and permeability drops to zero [55]. The resulting Eddy Current loss shows a peak during resonance [58] [12]. We can represent complex permittivity and complex permeability [72] [70] as:

The real part is responsible for the displacement current, whereas the imaginary part contributes to the conduction current. During Dimensional Resonance [12], the electric conductance of the magnetic material increases greatly. Hence the material acts like an electric conductor with a very low resistivity [58]. Although Magnetic conduction currents do not exist, Magnetic displacement currents can flow inside a magnetic material [13]. When the real permeability drops, the magnetic displacement currents are restricted and the magnetic susceptibility falls. This causes failure of the magnetic system. The associated loss tangents are:



Figure : Frequency dependance of Permeability

1. Residual Losses: Besides hysteresis loss [48] [44-46] and eddy current loss, several processes can contribute to losses [35-36] [13] [20] when the eddy currents are negligible and the applied flux density is extremely small. These stray losses [51] are independent of the flux density but they increase with frequency [58]. The associated loss tangent is .

The total loss tangent due to hysteresis loss [48] [44-46], eddy current loss and residual loss [51] [20] is expressed as:

In conclusion, the losses due to hysteresis [48] [44-46], Eddy currents [35-36], Piezomagnetism [35-36], Magnetoresistance [66], Magnetostriction [35-36] and other residual loss mechanisms [51] [20] can be expressed as heat losses across an effective resistance or conductance.

This chapter discussed the nature of Magnetic materials and the transmission of magnetic information using magnetic dipoles and Bulk Magnetization. The AC losses [20] of magnetic materials include hysteresis losses [48] [44-46], eddy current losses and residual losses [51] due to complex permeability and permittivity [35-36] [72] [70]. A literature review of Magnetic Transmission Lines [22-26] in context of recent research on Ferromagnetic Modeling and Simulation [18].

Chapter 2 will discuss the propagation of electromagnetic waves in anisotropic, inhomogeneous, dispersive [72] [44-46] [16] Ferromagnetic materials as dictated by the Maxwell’s Laws [55].

Chapter 3 presents three different models for Magnetic Elements: Reluctance Model, Permeance-Capacitance Model [73] [44-46] [32] [2] [3] and the Magnetic Transmission Line Model [22-26].

Chapter 4 is dedicated to computational electrodynamics [21] i.e. the low frequency and high frequency methods for solving Maxwell’s equations [55]. An overview of Finite Difference Time Domain method [68-69] [64] [43] [39] [9] is presented which solves partial differential equation using leapfrog method. The MEEP [52] simulator uses this method for evolving electromagnetic fields in anisotropic, inhomogeneous, dispersive [72] [16] Ferromagnetic materials.

## Literature Review

This section presents a literature review of Magnetic Transmission Lines [22-26] in context of the recent research on Giant Magnetoresistance [66], Magnetic Capacitance [74] [73], Magnetic Memory [41], Spintronic and Nanomagnetic Logic Devices [63] [42] [38] [34] [5] [15] [19] [30].

Faria [22-26] presented a Time and Frequency domain theory of multi-wire magnetic transmission lines based on the matrix theory of multi-conductor electric transmission lines. For magnetic transmission lines, transverse impedance and the longitudinal admittance determine the propagation constants for the wave modes [22-26]. Simulations showed that they exhibit super-luminal phase velocity and almost zero attenuation dispersion [72] [16]. He also established a relationship between voltages and currents at the multi-conductor transmission line ports by employing the transmission matrix techniques. Mathematical models were developed for studying the Frequency Domain Behavior of non-uniform Magnetic Transmission Lines [22-26]. Solutions to Electromagnetic equations were presented in the form of a superposition of natural modes of propagation [55]. The Magnetic Transmission Line exhibited the behavior of a high pass filter, blocking all DC signals. DC signals produce the most severe transients in Electric Transmission Lines [9]; which behave like a low pass filter. Moreover, he developed a model for ideal transformers using magnetic transmission line theory [22-26] [10].

Antonini [4] presented an in-depth analysis of meta-material transmission lines [10]. The ladder network structure of the transmission line was used to obtain dominant zeros and poles. This lead to a rational form of the two port network transfer function. The rational form of the transfer functions provided an efficient time-domain macro model; which accurately captured the physics of composite meta-material transmission lines [4] [10]. Caloz and Itoh [11] also presented non-linear [40] electromagnetic meta-material Transmission Lines [10] focusing on their complex permittivity and permeability [72]. They used the transmission matrix method to formulate equations for the dispersive [72] [16], distributed non-linear system [40] [8]. These results are very useful in understanding the complex dispersive [72] and radiative nature of Magnetic Transmission Lines [22-26].

Edwards and Steer [15] compared copper, ferrite meta-conductor and magnetized permalloy meta-conductor based coplanar waveguides. Magnetized ferrite layer provided some skin effect suppression compared to copper waveguide; however, permalloy provided the most uniform current profile. Some applications of Ferrite materials are high frequency phase shifters, circulators and isolators [53] [33] [27]. Phase shifters used in test and measurement systems can be controlled using the bias magnetic field. Electronically controlled phase shifters are used in phase array antennas for steering antenna beam in space. Microwave circulators [58] use ferrites to separate received and transmitted waves in radar systems [33] [16] [53]. Magnetized films also act as Radio Frequency selective limiters. Microwave Ferrite isolators are used for unidirectional transmission in plasma systems [49] [16] [27]. Their blocking capability protects precious microwave sources [54].

Neuber et al. [16], [17] presented gyromagnetic Non Linear Transmission Lines [62] [61] [71] constructed out of nickel-zinc (NiZn), magnesium-zinc (MgZn), manganese-zinc (MnZn) and yttrium iron garnet (YIG) ferrites [58] [53] [33] [27]. Biased Anisotropic Magnetic Transmission lines [22-26] functioned as microwave sources [54] because of Gyromagnetic Precession [71] [62] [61] [54]. Their performance strongly depended on Magnetic Saturation experienced at high biasing Field Strengths.

Paul [56] has presented Time domain and frequency domain Lumped Inductive-Capacitive Coupling Circuits [39] [18] for cross talk between different Electric Transmission Line Conductors. The generator-receptor model is well suited for studying Radiated/ Conducted Emissions and Susceptibility. Such models must be developed for Magnetic Transmission Lines [22-26] as well; to study their Electromagnetic Interference and Electromagnetic Compatibility [55].

Paul, Whites and Nasar [55] have presented a step-by-step method to solve the Maxwell’s equations in sinusoidal steady state; due to a given current distribution in a homogeneous, linear, isotropic medium. First, magnetic potential field is calculated at all desired points in space, due to the current distribution. The curl of the magnetic potential field is used to obtain the magnetic field. The Divergence of the magnetic potential field is used to obtain the scalar Electric Potential. In turn, the magnetic potential field and the gradient of the electric potential are used to derive the Electric field. The procedure is much more complicated for waveguides in inhomogeneous, anisotropic, and non-linear media [40] [8]; hence, numerical methods [21] are suggested where a closed form solution is not possible.

Er-Ping [21] has discussed a wide range of standard time and frequency domain Computational Electromagnetics [14] [12] [21] Methodologies. Time Domain Methods [39] include Analytical Methods, Finite Difference Methods (FDTD) [64] [43] [9], Finite Integral Methods (FIT), Finite Volume Methods (FVTD), Fast Multipole Method (FMM), Partial Element Equivalent Circuit Method (PEEC), Transmission Line Method (TLM) [43] etc. Frequency Domain Methods include Method of Moments (MoM), Finite Element Method (FEM), Geometric Theory of Diffraction (GTD), Physical Theory of Diffraction (PTD) etc. He compared Finite Difference Methods, Method of Moments and Finite Element Method, in respect of Principle, geometry materials, Meshing, Matrix Equation and Boundary Treatment. He gave a list of commercially available simulators along with some common applications like high-speed electronics [58], photonics [12] [15], microwave circuits [16], integrated circuits and Antennas. The Finite Difference Method can obtain response over a broad band of frequencies for many non-linear [40] [8] and inhomogeneous media without using matrix equations [9] [43]. This method is well suited for simulation of dispersive [72] [16], non-uniform Magnetic Transmission Lines [22-26].

# Wave Propagation in Magnetic Materials

This chapter will discuss the propagation of electromagnetic waves in anisotropic, inhomogeneous, dispersive [72] [16] Ferromagnetic materials as dictated by the Maxwell’s equations [55].

## Plane Wave Propagation

Ideal Magnetic Transmission Lines [22-26] can be modeled as linear, isotropic, homogeneous media which follow Maxwell’s equations [55]:

1. Ampere’s Law [55]
2. Faraday’s Law [55]
3. Gauss’ Laws

subject to the following boundary conditions [55]:

1. The perpendicular components of **B** and **D** follow these conditions:
2. The parallel components of **H** and **E** follow these conditions:

The solution is given by the Helmholtz Equations [55]:

For sinusoidal steady state:

The propagation constant () dictates the wave propagation in the medium. The attenuation constant () represents the loss or attenuation of fields. The skin depth () is defined as the penetration measured from the surface at which the amplitude reduces by a factor of 1/e:

The phase constant dictates the phase velocity (u) and wavelength (𝜆):

The ratio of matching Electric Field Intensity and Magnetic Field Intensity determines the intrinsic impedance of the material:

For lossless magnetic materials with very small ,

where , , and represent the free space phase constant, phase velocity wavelength and intrinsic impedance respectively.

Considering plane wave propagation in the z direction, the solution is:

## Power Flow Analysis

The power flow density of an electromagnetic wave is given by the Poynting vector **S**. It has the units of W/m2. The Poynting flux is indicative of the amount of power flowing across a surface:

The expression can be expanded using the following formula:

The flow of Poynting flux can be separated into the Ohmic Power dissipation, Electric Power flow and Magnetic Power flow:

From these expressions, it is clear that the Electric Energy and Magnetic Energy of a system is:

The average power transported per unit area is the Intensity of the Electromagnetic Wave:

Electromagnetic Waves also carry momentum and the momentum density stored in the fields is

The Momentum transferred to a surface results in a radiation pressure

# Magnetic Circuit Modeling

In this chapter, three different Magnetic circuit models will be presented: The Reluctance Model, The Permeance-Capacitance Model [73] [44-46] [32] [2] [3] and The Magnetic Transmission Line Model [22-26]. It is understood that magnetic monopoles do not exist and Magnetic conduction current cannot flow. Any reference to the flow of Magnetic displacement current is meant to indicate the flow of Magnetic Displacement Current i.e. the rate of change of Magnetic Flux.

The Reluctance Model is the oldest and most popular model, even though it is not a power invariant model [28]. It only has one component called the Magnetic Reluctance which resists the flow of Magnetic Flux.

The Permeance-Capacitance Model [73] [44-46] [32] [28] [2] [3] overcomes the weaknesses of the Reluctance Model by considering the rate of change of Magnetic Flux as the Magnetic displacement current. It is a power invariant model [28] because it correctly encompasses the transformation of Magnetic and Electric Energy [32]. This model has the shortcoming that it does not incorporate Electric Energy Storage and Electromagnetic losses in a Magnetic material [35-36] [20].

The Magnetic Transmission Line [22-26] model improves the Permeance-Capacitance Model [73] [44-46] [32] [2] [3] [28] by including a component for Electric Energy Storage and a component for magnetization, polarization and conduction losses [35-36] [20].



Figure : A Magnetic core excited by an electric current

## Reluctance Model

This section

H. A. Rowland’s Law (1873) [55] is the counterpart of G. Ohm’s Law (1827) for Magnetic circuits. Complex Reluctance Model defines Magnetic reluctance as the ratio of sinusoidal Magnetomotive Force and sinusoidal Magnetic Flux.

Lossy Complex Magnetic Reluctance is non-linear and varies with the magnetic field. It resists both Magnetic flux and changes in Magnetic flux.



Figure : Reluctance model for Magnetic Core

In 1969, R. W. Buntenbach proved that the Reluctance model [55] is not power invariant [28]. Reluctance Power Loss cannot be calculated using Joule Heating Law (1842) analogy due to dimensional inconsistency:

Hence this is not an accurate model for Power and Energy Flow.

## Application

This section presents the reluctance model for a Compounded DC Generator [11] with both a series and a shunt field winding. The series field inductance has turns. The series field winding resistance is represented by . The shunt field winding inductance has turns. The shunt field winding resistance is represented by . The armature winding resistance is represented by .

The Electric circuit equations are

The magnetic circuit equations are

The generated electric voltage is related to the Magnetic Flux and rotor speed by the following equation



Figure : Model for Cumulatively Compounded DC Motor

The Reluctance Model preserves the integrity of the machine’s geometry. It decouples the electrical system from the magnetic system. The magnetic paths in the core are represented using reluctance elements.

The Pockels and Kerr Non-linearity model (1875) explains how and can change as a function of the field intensity [40] [48]. Ferromagnetic materials are non-linear [48] [8] [39] as their permeability varies with the strength of applied field intensity. At high magnetic field intensity, the material saturates, limiting further increase of Magnetic Flux [48]. Hence, the susceptibility decreases rapidly.



Figure : Simulink Model for Cumulatively Compounded DC Generator

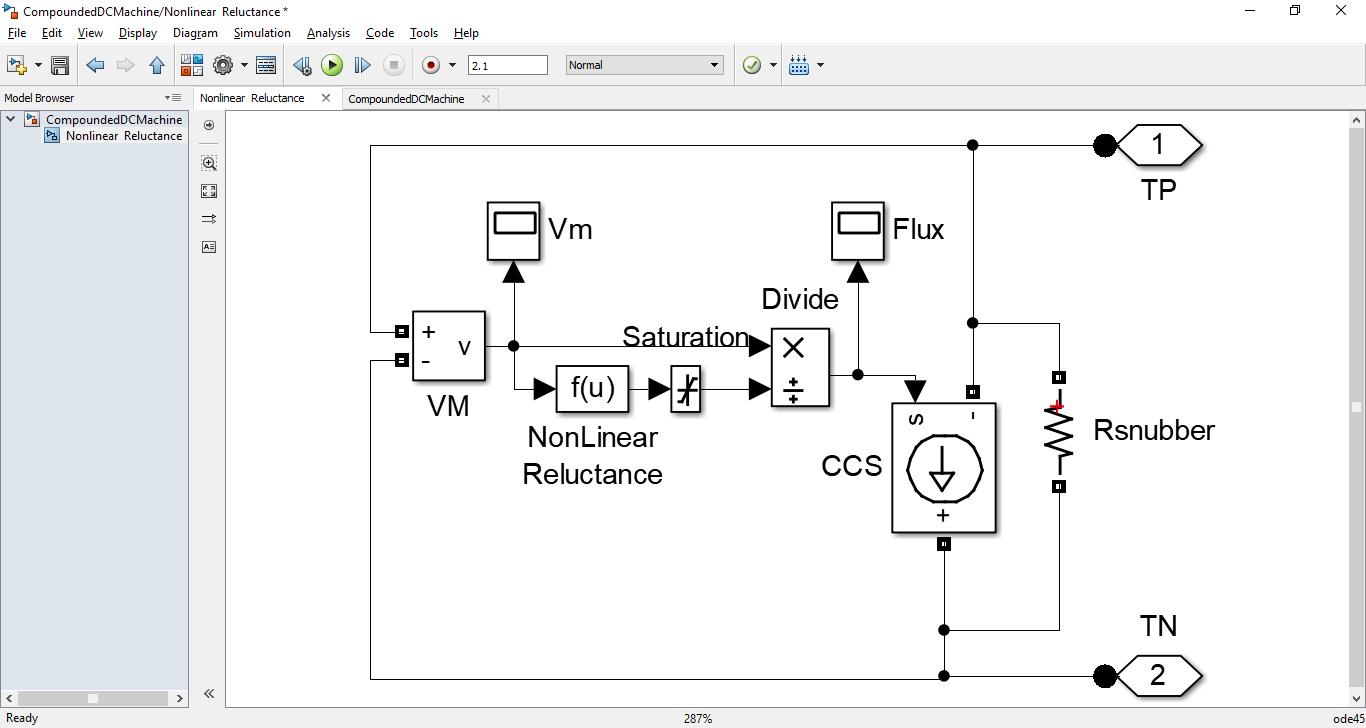


Figure : Simulink Model for Nonlinear Permeance

RA=0.19 Ω, RS=0.02 Ω, RF=20-50Ω, NF=1000 turns, NS=20 turns, nm=500:500:2000 rpm



Figure : Evolution of Field Currents, Net MMF, Generated EMF and Terminal Voltage upon change of Rotor speed



Figure : Variation of Terminal Voltage with rotor speed

## Permeance-Capacitance Model

This section presents the power invariant Permeance-Capacitance model for a Transformer based on the gyrator theory. The model is valuable for modeling nonlinear magnetic materials with hysteresis losses.

B. Tellegen’s Gyrator theory (1948) was devised to describe power invariant transformation of magnetic and electric quantities in a transformer [32] [3] [28]. The dual effort and flow quantities are related by the gyration constant (N). According to M. Faraday’s Law (1831) [55], Electric Voltage is responsible for producing Magnetic Displacement Current which is defined as the rate of change of magnetic flux.

Magnetic Displacement Current is the rate of change of Magnetic Flux which results from the polarization of Magnetic Dipoles. For a magnetic core, the magnetic displacement current and Magnetomotive Force are given by:

According to A. Ampere’s Law (1861) [55], Magnetic Voltage is responsible for producing Electric Conduction Current [55].

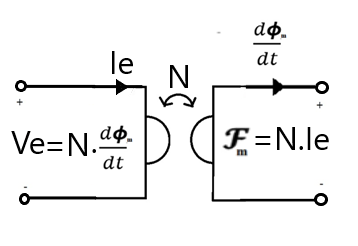


Figure : Gyrator Model for power invariant transformation of Electric and Magnetic quantities

R. W. Buntenbach proposed Power Invariant Permeance-Capacitance Model (1969) [73] [44-46] [32] [28] [2] [3] to replace Reluctance Model.

Magnetic Permeance [44-46] [32] [2] [3] is defined as a magnetic capacitor which stores magnetic flux measured in Volt-seconds.

It resists changes in Magnetic voltage.

This Permeance is measured in units of Henry. It is closely related to Magnetic Reluctance and Magnetic Inductance of the core.

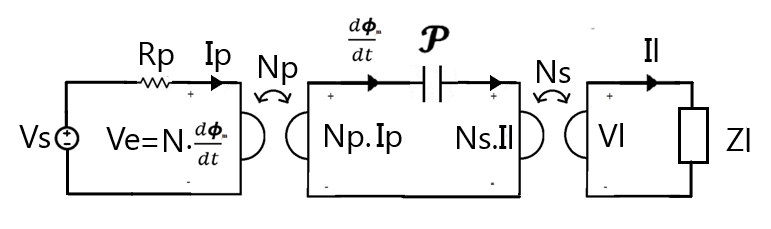


Figure : Permeance-Capacitance model for Transformer

## Application

This section presents a Permeance-Capacitance Model [73] [44-46] [32] [2] [3] for a full bridge Isolated Buck Converter. The electrical circuit is shown below.

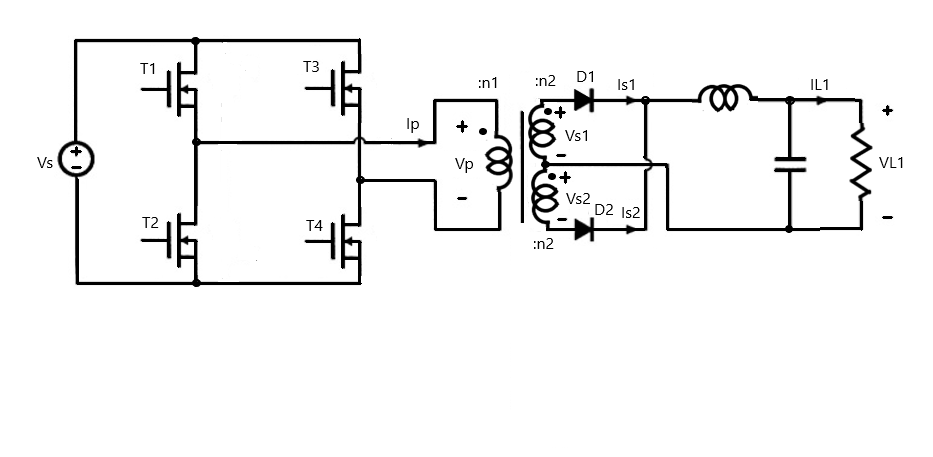


Figure : Electrical circuit for Full Bridge Isolated Buck Converter

The switching table for the switches and diodes is given below.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
|  | Transistors | | | | Diodes | |
| Time Interval | T1 | T2 | T3 | T4 | D1 | D2 |
|  | ON | OFF | OFF | ON | ON | OFF |
|  | OFF | ON | OFF | ON | ON | ON |
|  | OFF | ON | ON | OFF | OFF | ON |
|  | ON | OFF | ON | OFF | ON | ON |

The design parameters are given in the table below

|  |  |  |
| --- | --- | --- |
| Parameter | Symbol | Value |
| Source Voltage |  | 160 V |
| Load 1 Voltage |  | 5 V 5% |
| Load 1 Current |  | 100 A 5% |
| Core cross-sectional area |  | 2.26cm2 |
| Core Magnetic Path Length |  | 9.58 cm |
| Peak Flux Density |  | 0.08 T |
| Core relative Permeability |  | 3500 |
| Core Resistivity |  | 0.02 Ωm |
| Switching Frequency |  | 150 kHz |
| Duty Cycle | D | 0.75 |

The Design Procedure has the following steps:

1. Applied Primary winding flux
2. Turns of Primary winding
3. Turns of Secondary windings
4. Core Permeance
5. Core Resistance
6. Load Filter Design

The equivalent circuit for the converter is shown below. It shows the primary voltage as a PWM Voltage source . The primary winding resistance is represented by . The primary current is converted to Magnetomotive force across the gyrator with gyration constant . The nonlinear core Permeance is represented by element . The secondary side consists of two gyrators with gyration constant Each gyrator senses the Magnetic voltage and generates proportional secondary current. The secondary side circuit consists of a rectifier circuit and a filter circuit to provide constant voltage and current to the load.

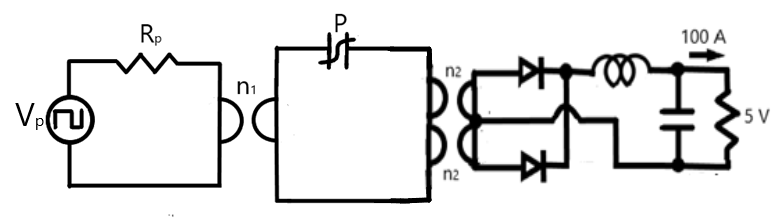


Figure : Equivalent converter circuit with gyrators and nonlinear core Permeance

The Simulink Model for the nonlinear Permeance is shown below.

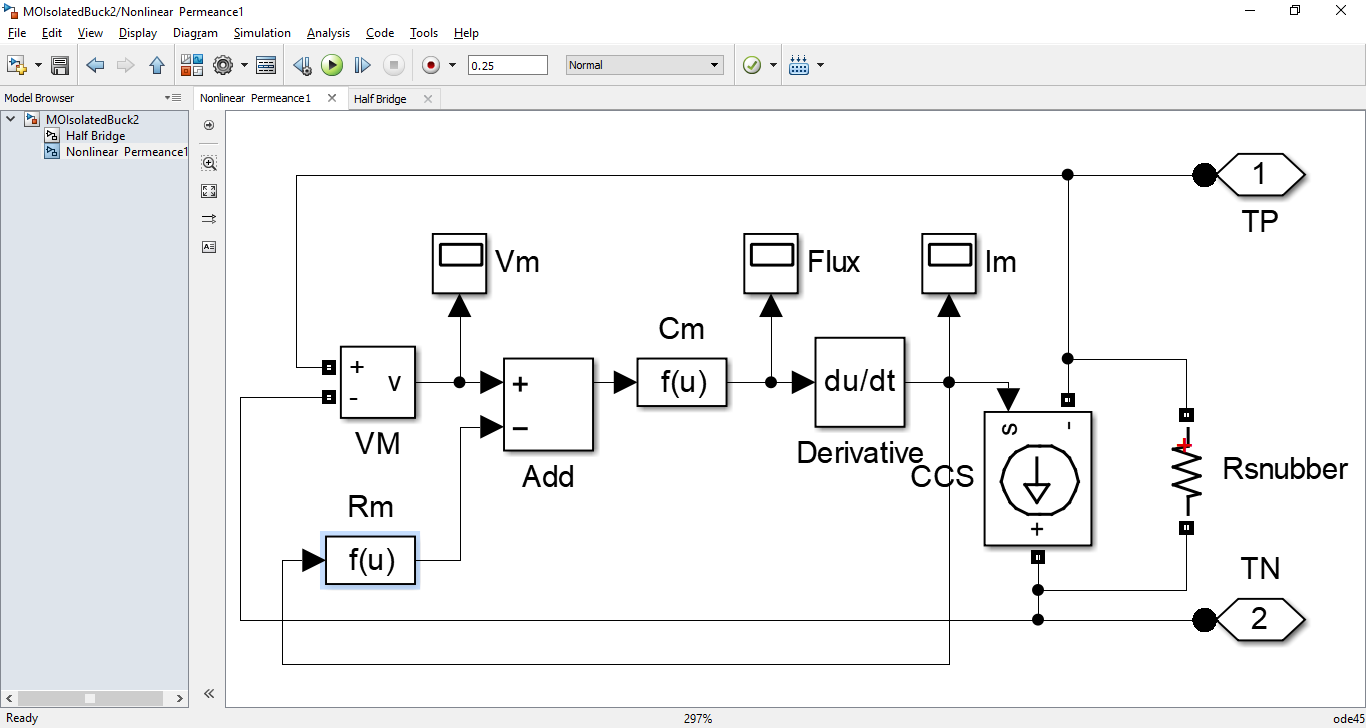


Figure : Simulink Model for nonlinear Permeance

The Flux response of nonlinear Permeance for voltage variation is recorded in the figure below. The slope of the Flux-voltage curve gives the instantaneous Permeance. The area between the two curves represents the magnetic hysteresis loss.



Figure : Variation of Permeance Flux versus Permeance Magnetic Voltage

The designed Transformer was excited by a sinusoidal voltage source of amplitude 100 V. The transformer was loaded with a resistive load of 1 Ω. The output voltage and current are plotted below. As seen, the output voltage and current shows large spikes when the Permeance experiences large voltages.



Figure : Transformer voltage and current response for sinusoidal excitation and resistive load

The Simulink Model for Isolated Buck Converter is shown below.

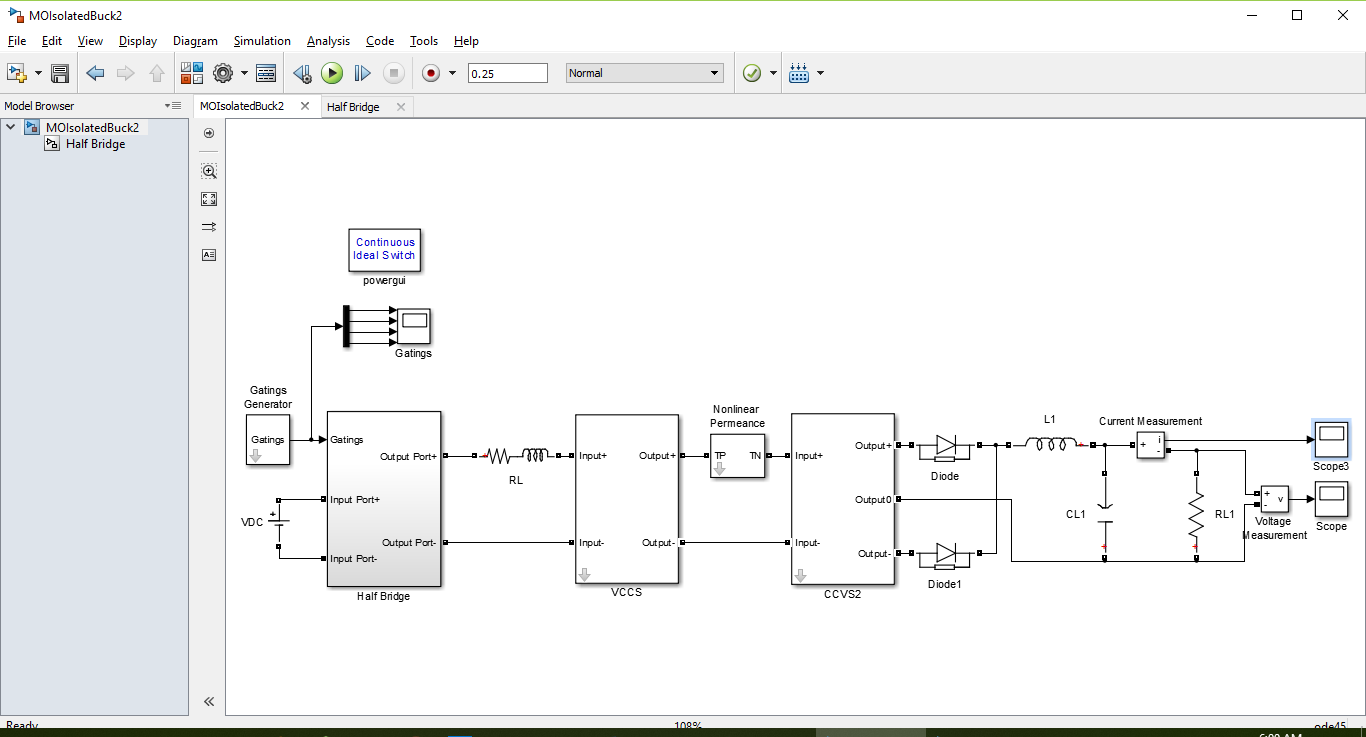


Figure : Simulink Model for Full Bridge Isolated Buck Converter

The Simulink Models for primary and secondary winding gyrators are shown below.

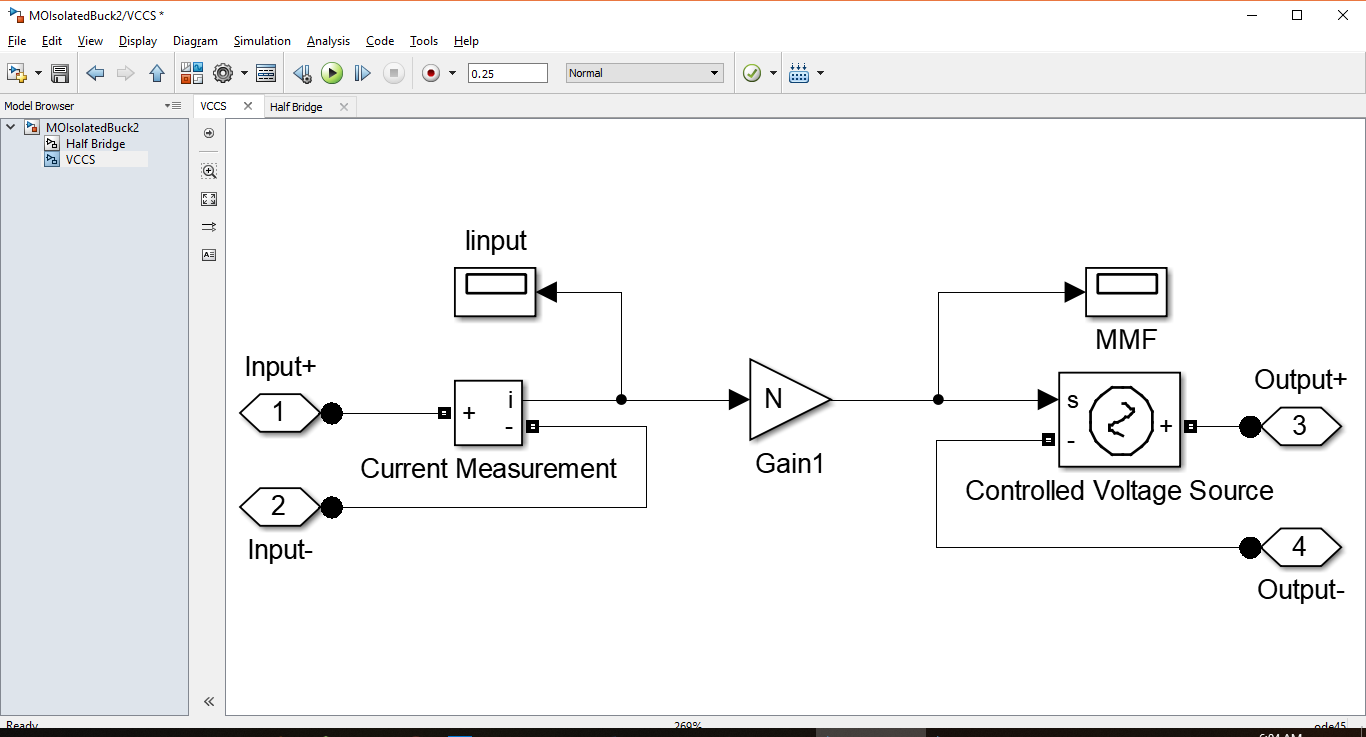


Figure : Simulink Model for Primary winding gyrator

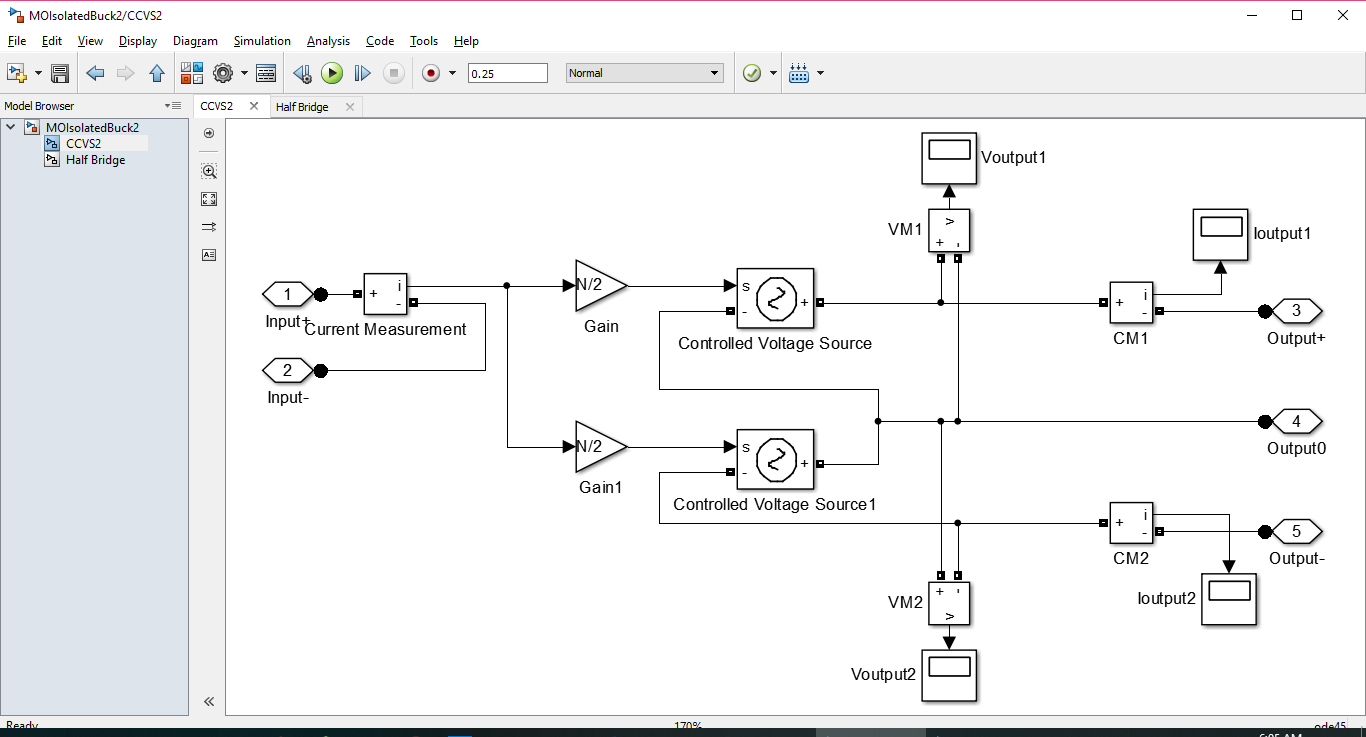


Figure : Simulink Model for secondary winding gyrator

The primary winding Electric voltage and Electric current are plotted below.



Figure : Primary winding voltage and current

The load Electric voltage and Electric current are plotted below.



Figure : Load voltage and current

The Permeance Magnetic voltage and Magnetic displacement current are plotted below.



Figure : Permeance voltage and Current

## Magnetic Transmission Line Model

This section presents the third model for magnetic elements called the Magnetic Transmission Line Model. This model is based on the age old Electric transmission line model [22-26]. Like the Permeance-Capacitance Model, it also considers flux rate as the effective magnetic displacement current whereby magnetic permeability plays a similar role to electric conductivity by enhancing the magnetic displacement current inside the magnetic material.

J. A. B. Faria and M.P. Pires presented Magnetic Transmission Line Model [22-26] (2012) based on Electric Transmission Line Model. The propagation of electromagnetic waves is governed by the Maxwell’s Equations [55]:

Analogous to the scalar Electric Potential, scalar magnetic potential can be defined as

The Magnetic Displacement Current is defined as the rate of change of magnetic flux :

The per unit length transverse magnetic inductance represents a magnetic Energy storage element. It is defined in terms of per unit length Magnetic charge and scalar magnetic voltage as

The per unit length longitudinal capacitance represents an Electric Energy storage element [73]. It is defined in terms of electric displacement flux and magnetic displacement current as

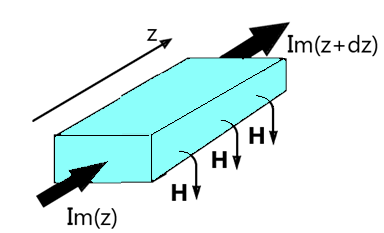


Figure : A section of Magnetic Transmission Line transmitting flux in z-direction

Assuming TEM-guided propagation in z-direction (), the relation between the magnetic voltage and magnetic displacement current for a homogeneous magnetic transmission line [22-26] is derived by substituting the previous expressions in the Maxwell’s Equations [55].

The resulting Transmission Line Equations are

A forward travelling and a backward travelling wave can simultaneously exist on the transmission line. The solution for the Magnetic voltage and Magnetic displacement current is

The propagation constant is defined as

The characteristic impedance is the ratio of Magnetic displacement current to the Magnetic Voltage. It is calculated as

The average power flow in the Magnetic Transmission Line [22-26] can be represented in terms of three distinct components: the average power in the forward travelling wave, the average power in the backward travelling wave and the dissipated power.



Figure : Equivalent circuit model for magnetic transmission line

In a non-ideal magnetic transmission line [22-26], magnetic voltage drop can be accounted by including magnetic reluctance/ conductance. It represents all the magnetization, polarization and conduction losses [20] due to electric conductivity, complex permittivity and complex permeability [72] [70] [35-36]. Magnetic Inductance and Magnetic Capacitance are energy storage elements in this model [74] [73].

Energy is dissipated in Magnetic Conductance:

Electrical Energy is stored in Magnetic Capacitance [74] [73]; and Magnetic Energy is stored in Magnetic Inductance [22-26].

The resulting Magnetic Transmission Line Equations [22-26] are:

Assuming sinusoidal steady state, the equations can be expressed in terms of phasor quantities as follows:

The Magnetic Transmission Line Equations [22-26] can be solved just like Electric Transmission Line Equations. The solutions are compared in the table below.

|  |  |
| --- | --- |
| Electric Transmission Line | Magnetic Transmission Line |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

For Electric Transmission Lines of same geometry described by and matrices, the magnetic Transmission Line parameter matrices are closely related:

Magnetic cores are often manufactured using layers of laminated magnetic sheets to prevent the flow of Eddy Currents. In such materials, magnetic flux from one transmission line can link with a neighboring magnetic transmission line [22-26] and disturb the information [21]. The Magnetic Transmission Line Model [22-26] can be extended to the generator-receptor Magnetic Transmission Line model [22-26]. This is well suited for studying Electromagnetic Coupling of Magnetic Transmission Lines [22-26] which are in close proximity.



Figure : Equivalent circuit model for cross-talk between neighbouring Magnetic Transmission Lines

## Summary

This chapter presented three different models for modeling magnetic elements. The age old reluctance model based on the Ohm’s law analogy was found to violate power invariance property hence a new model was devised based on the gyrator theory. The Permeance-Capacitance model uses a nonlinear permeance to model nonlinearity and hysteresis losses of magnetic materials. The third model was the magnetic transmission line model which is the most accurate model for modeling dispersive, inhomogeneous and lossy magnetic cores. The three models are summarized in the table below.

|  |  |  |  |
| --- | --- | --- | --- |
|  | **Reluctance Model** | **Permeance-Capacitance Model** | **Transmission Line Model** |
| **Conserved Quantity** | ? | Magnetic Flux  [Volt-Second] | Magnetic Flux  [Volt-Second] |
| **Flow Variable** | Magnetic Flux  [Volt-Second] | Rate of change of Magnetic Flux [Volt] | Rate of change of Magnetic Flux [Volt] |
| **Effort Variable** | Magnetomotive Force [Ampere] | Magnetomotive Force [Ampere] | Magnetomotive Force  [Ampere] |
| **Energy Dissipation Element** | Magnetic Reluctance [] | ? | Magnetic Conductance  [Ohm] |
| **Electrical Energy Storage Element** | ? | ? | Magnetic Capacitance  [Farad] |
| **Magnetic Energy Storage Element** | ? | Magnetic Permeance  [Henry] | Magnetic Inductance  [Henry] |

# Computational Electromagnetics

This chapter discusses the different time domain and frequency domain methods for solving Maxwell’s Equations [55] [21] [39] [1].

## Methods for solving Maxwell’s Equations

The Maxwell’s Equations can be solved in time domain and frequency domain by solving Partial Differential Equations or Integral Equations [55] [39]. Some of the methods are listed in the table below.

|  |  |
| --- | --- |
| **Method** | **Remark** |
| Adaptive Integral Method (AIM) | Provides efficient iterative procedure for matrix algebra for linearized version of Maxwell’s equations. |
| Analytical closed form techniques | Approximate methods are used in cases with high degree of symmetry. Closed form solutions are not always possible. |
| Bi-conjugate gradient method with Fast Fourier Transform (BCG-FFT) | Useful in solving complex matrix equations resulting from the interactions of electromagnetic waves with surfaces. |
| Boundary Element Method (BEM) | Discretizes boundary elements to solve low frequency or steady state AC problems. |
| Conjugate Gradient Method (CGM) | Uses iterative method of conjugate gradients to solve systems involving large and sparse matrices. |
| Fast Multipole Method (FMM) | Uses approximations to solve for far field scalar potential. |
| Finite Difference Frequency Domain (FDFD) | Uses optimal discretization to solve time harmonic versions of linearized Maxwell’s equations. |
| Finite Difference Time Domain (FDTD) | Maxwell’s Equations are linearized using finite differences. Entire volume is uniformly discretized and fields are evolved by time stepping. Transient analysis of sharp edges increases resolution and computational time. |
| Finite Element Method (FEM) | Entire volume is non-uniformly discretized into homogeneous sub-regions. Field are computed by minimizing energy functions. |
| Finite Integration Technique (FIT) | Integral version of Maxwell’s Equations are solved in a non-uniformly meshed volume with very high resolution. |
| Finite Volume Time Domain (FVTD) | Entire volume is non-uniformly discretized and fields are evolved by time stepping. |
| Generalized Multipole Technique (GMT) | Surface charges and currents are used to determine frequency domain analytical field solutions using method of weighted residuals. |
| Geometrical Optics (GO) | Used for exact ray tracing for light wave propagation in optical media. |
| Geometrical/ Uniform Theory of Diffraction (GTD/ UTD) | Used for high frequency ray tracing and asymptotic solutions are used for solving diffraction problems. |
| Hybrid Lumped Circuit and Quasi Transmission Line Method | A hybrid method to accurately model lumped elements in microwave applications. |
| Method of Moments (MoM) | Wire mesh currents and patch surface currents are used to analyze complex inhomogeneous structures through the method of weighted residuals. |
| Multiple Multipole (MMP) | Generalized point matching is used to find a series of homogeneous domain analytic solutions that compose the field. |
| Partial Element Equivalent Circuit (PEEC) | A circuit of small electrical elements is used to approximate PCB radiation patterns. |
| Shooting Bouncing Rays (SBR), Physical Optics (PO), Physical Theory of Diffraction (PTD) | Planar surfaces are irradiated with electromagnetic field by transmitters. Receivers use detected radiation to compute local field. |
| Singularity Expansion Method (SEM) | Laplace Transform with complex frequencies is used to detect characteristic resonance of complex scatterers. |
| Spectral Domain Approach (SDA) | Spatial Fourier Transform is used to solve fields in spectral domain. |
| Transmission Line Method (TLM) | Complex nonlinear materials can be modeled using virtual transmission lines. The Voltage and current inform about the fields. |
| Vector Parabolic Equation Technique (VPE) | Useful in radio communication systems. |

After this brief review of Computational Electromagnetics, the next section discusses Finite Difference Time Domain Method which will be used to simulate nonlinear, anisotropic, inhomogeneous Magnetic Transmission Lines.

## Introduction to Finite Difference Time Domain Method

Finite Difference Time Domain Method (FDTD) or K. S. Yee’s Method (1966) is a differential numerical modeling technique for computational electrodynamics [68-69] [39] [21] [43] [64]. Finite Difference Time Domain Method [9] discretizes space into a grid of small elements called Yee Lattice (1966) [68-69] [64] [43]. Each element can have a different conductivity, permittivity and permeability [43] [39].



Figure : Location of different Field components in a Yee Cell

J. C. Maxwell’s Equations (1861) [55] are discretized using central difference approximations to the space and time partial derivatives. For example, Faraday’s Law can be expanded as follows:

Similarly, Ampere’s Law can be approximated as follows:

The different field components at a grid location are stored in the edges and faces of a cubic element called Yee’s Cell. They are evolved in discrete time steps [68-69].

The location of field components and the central difference operations implicitly enforce the two Gauss’s Laws [55].

The finite region of space must always be terminated with some boundary conditions. Some examples include:

1. Bloch-periodic Boundaries are used for simulation of periodic structures . Periodic Bloch Boundaries copy the field component at one cell’s edge and reinject them at a neighboring cell’s edge.
2. At Metallic Walls, all fields are forced to be zero hence it is a perfect reflector with zero absorption and zero skin depth.
3. Perfectly Matched Layers allow all the fields to pass through with minial reflection. These absorbing boundary conditions (ABCs) absorb almost all of the incident field.

## Introduction to MEEP Simulator

This section gives a brief introduction to MEEP [52] simulator designed for solving the Maxwell’s Equations [55] using discrete time stepping. MEEP [52] is a script based Simulator for modeling the time domain [39] and frequency domain behavior of a variety of arbitrary materials.

1. A fully scriptable open source C++ interface is provided for generating optimized algorithms.
2. The use of normalized units for solving Maxwell’s Equations provides exceptional resolution in frequency and time domain. The simulator can be run on multicore supercomputers to speed up execution and transient analysis.
3. A Material Library with sample data for several materials is provided in libraries for building accurate test structures.
4. A wide variety of electric or magnetic soft current sources can be simulated. G. Green’s Functions (1835) give the Field Patterns from a localized point source at a particular frequency .
5. A frequency domain solver is also provided for multidimensional Fourier transformation (1822) and the decomposition of fields into travelling modes [59]. The 3 Dimensional Discrete Fourier transform (1822) of the response to a short impulse can give useful information about the transmitted power and losses [35-36] [59] [50] [21].
6. Averaging, symmetry and integration are allowed in cylindrical and rectangular three dimensional coordinates. Hence different homogeneous/inhomogeneous structures can be built inside the space. Electric/ Magnetic/ Thermal Energy Density, Poynting Flux etc. can be evaluated. The Transmitted Power can be computed using the integral of Poynting Vector (1884); over a surface on the far end of the transmission line. Transmitted power and incident power can be used to find power losses in transmission line.
7. The fields can be printed as image or video files through Data Visualization features.

MEEP [52] can simulate anisotropic, dispersive [72] [16], non-linear [40] and gyrotropic media [54].

1. Anisotropic Media: For anisotropic media, non-diagonal susceptibility tensor is used to relate Polarization/ Magnetization and Field intensity.

1. Dispersive Media: Drude-Lorentzian Model (1900) models frequency dependent permittivity and permeability [72] [16]. It explains the electrodynamic properties of metals by regarding conduction band electrons as non-interacting electron gas. When the material is excited by an external source of resonant frequency, the material absorption loss increases greatly. Electromagnetic Energy is converted into other forms of energy. Flux Densities contain terms for infinite frequency response and frequency dependent Polarization vector [72].

and are represented as a sum of harmonic resonances [72] [12] and a term for frequency independent electric conductivity.

is the electrical/magnetic conductivity. is the oscillator strength, is the angular resonance frequency, is a damping factor.

1. Nonlinear Media: The Pockels and Kerr Non-linearity model (1875) explains how and can change as a function of the field intensity [40] [48]. Ferromagnetic materials are non-linear [48] [8] [39] as their permeability varies with the strength of applied field intensity. At high magnetic field intensity, the material saturates, limiting further increase of Magnetic Flux [48]. Hence, the susceptibility decreases rapidly.

sum is the Pockels effect constant; whereas sum is the Kerr effect constant.

1. Gyrotropic Media: Landau-Lifshitz-Gilbert model (1955) describes the precessional motion of saturated magnetic dipoles in a magnetic field [62] [54].

describes the linear deviation of magnetization from its static equilibrium value. Precession occurs around this unit bias vector . represents oscillator strength, is the angular resonance frequency, is the oscillator damping factor.

MEEP uses normalized units for solving Maxwell’s Equations. A conversion scheme from SI units to MEEP units is shown in the table below.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **Property** | **Symbol** | **Reference Scale in SI Units** | **SI to MEEP**  **Conversion Factor** | **Normalized MEEP Units** |
| **Length** |  | 1.00000 m | = 1.00000 | 1 |
| **Speed of Light** |  | 2.99792 | = 3.33564 | 1 |
| **Current** |  | 1.00000 A | = 1.00000 | 1 |
| **Time** |  | = 3.33564 s | = 2.99792 | 1 |
| **Frequency** |  | = 2.99792 Hz | = 3.33564 | 1 |
| **Permittivity** |  | 8.85418 | = 1.12940 | 1 |
| **Permeability** |  | 1.25663 | = 7.95774 | 1 |
| **Electric Field Intensity** |  | = 3.76730 | = 2.65441 | 1 |
| **Electric Flux Density** |  | = 3.33564 | = 2.99792 | 1 |
| **Magnetic Field Intensity** |  | = 1.00000 | = 1.00000 | 1 |
| **Magnetic Flux Density** |  | = 1.25663 | = 7.95774 | 1 |
| **Electric Conductivity** |  | = 2.65441 | = 3.7673 | 1 |
| **Electric Current Density** |  | = 1.00000 | = 1.00000 | 1 |
| **Energy Density** |  | = 1.25663 | = 7.95774 | 1 |
| **Poynting Vector** |  | = 3.76730 | = 2.65441 | 1 |
| **Courant Factor** |  | = 3.33564 | = 2.99792 | 1 |

# Magnetic Transmission Line Simulation

This section presents an application of Magnetic Transmission Line Model by predicting the response of a wideband transformer. The results of the Transmission Line model will be verified by simulating the structure in MEEP simulator [52].

The Electromagnetic simulations will be carried out in MEEP [52] Simulator which is a script based Finite Difference Time Domain [68-69] [64] [43] [9] Electromagnetic Fields Simulator for solving Maxwell’s Equations [55].

Lumped circuits [18] are used for studying linear, time invariant, distributed systems like Magnetic Transmission Lines [22-26]. The distributed parameters can be calculated using mathematical formulas. MATLAB will be used for modeling the time and frequency domain behavior of Magnetic Transmission Lines [22-26] in terms of simplified Lumped Circuits.

Finite Difference Time Domain [68-69] [64] [43] [9] Electromagnetic Field MEEP [52] Simulations will be carried out for dispersive [72] [16] Magnetic Transmission Lines [22-26] in anisotropic, inhomogeneous, non-linear media [40] [65] [39]. The Magnetic Transmission Lines [22-26] will be constructed using Drude-Lorentz susceptibility models for ferromagnetic conductors like Nickel, Iron and Cobalt alloys. The Transmission Lines will be excited using continuous point sources. The terminations can be modeled by Perfectly matched layers for Surge Impedance Loading; or as perfect reflectors for no load. Different Transmission Line structures can be simulated like the Wideband Transformer [67] [65] [31] [29] [14] [17] [35-36] and Transmission Line Transformer.

## Simulation of Magnetic Transmission Line in MEEP

In order to study their frequency response to continuous sources, Finite Difference Frequency Domain [1] Electromagnetic Field MEEP [52] Simulations will be carried out. The multi-dimensional Fourier transform and mode decomposition will be used for this study. In order to simplify analysis, the Distributed System will be linearized to obtain a lumped model. The frequency Domain Behavior will also be studied using Transfer Function of Equivalent T-model Transmission Line circuit.

Multi-conductor Transmission Lines introduce many complexities like capacitive/ inductive coupling. MEEP [52] Simulations and MATLAB Lumped Circuit Simulations [18] will be carried out for studying cross talk between Conductors of multi-wire Magnetic Transmission Lines.

As in the case of Electric Transmission Lines, Power Flow Equations can be developed for Magnetic Transmission Lines [22-26] in terms of Lumped parameters; like per unit length transverse impedance and the per unit length longitudinal admittance. The results can be verified using electromagnetic simulations.

The Electromagnetic MEEP [52] Simulations will help to probe the stored Electric/ Magnetic Energy Density, geometric parameters, per unit length losses and Transmission Efficiency of Magnetic Transmission Lines. Among the different magnetic materials, the best alloy will be chosen based on desired performance metrics. A suitable candidate must exhibit minimal radiation and line losses. The transverse impedance and longitudinal admittance dictate the propagation of wave modes in magnetic transmission lines [22-26]. Simulations will be used to estimate per unit length transverse inductance and longitudinal capacitance [73], which contribute to the transverse impedance and longitudinal admittance respectively. These parameters are pivotal in determining the lumped model of the distributed Transmission Line system.

The Magnetic Transmission Lines [22-26] will be excited by continuous sources to examine their Frequency Response. The Fourier Transform will decompose the Fields into the various travelling wave modes. This will aid the study of the effects of magnetic hysteresis [48] [44-46] and saturation on power quality [9]. The T-model Equivalent Magnetic circuits [18] and coupled equations will be used to simplify analysis of the transient [9] and steady state behavior. According to theory, Magnetic Transmission Lines [22-26] must exhibit the behavior of a high pass filter, blocking all DC signals. DC signals produce the most severe transients in Electric Transmission Lines [9]; which behave like a low pass filter. However, this also implies that Magnetic Transmission Lines [22-26] must be operated at higher frequencies than Electric Transmission Lines. Poorly designed Magnetic Transmission Lines [22-26] may amplify high frequency noise which can be damaging for the power system. The imaginary part of Transmission Line Magnetic Reluctance, which is a strong function of frequency, contributes to line losses. Hysteresis losses [48] [44-46] also increase significantly at higher frequencies [20] [9] [35-36]. Hence, an appropriate frequency must be chosen, considering the complex nature of the magnetic material.

The study of capacitive/ inductive coupling in Multi-Conductor Transmission Lines will provide useful knowledge about the Radiated/ Conducted Emissions and Susceptibility. The generator-receptor model is well suited for studying Electromagnetic Interference and Electromagnetic Compatibility of Magnetic Transmission Lines [22-26]. The results can be compared with mathematical formulas to build linear circuit models [18] for cross talk between Magnetic Transmission Lines [22-26]. The aim will be to minimize Electromagnetic Radiation; that can be picked up by intentional receivers like Radio and Television; or unintentional receivers like digital Computers. This will prevent malfunction of the sensitive electronic equipment.

Power Flow Equations for Magnetic Transmission Lines [22-26] will help to compare the Electromagnetic and Magnetic circuit models. The Power Flow will be represented in the form of Magnetic displacement current and Magnetic Voltage for circuit Model. For the Electromagnetic Model, the Power Flow will be represented in the form of Magnetic Field and Electric Field. Accurate Estimation of Lumped parameters; like per unit length transverse impedance and the per unit length longitudinal admittance is necessary for producing a valid lumped magnetic circuit [18] for Magnetic Transmission Lines [22-26].

Figure : Overview of MEEP algorithm for simulation of Magnetic Transmission Line

The geometry of the simulated Magnetic Transmission Line is shown below. The electric current source is represented by a current loop at z = 0 mm. The magnet flux and magnetic displacement current flows in the z-direction.

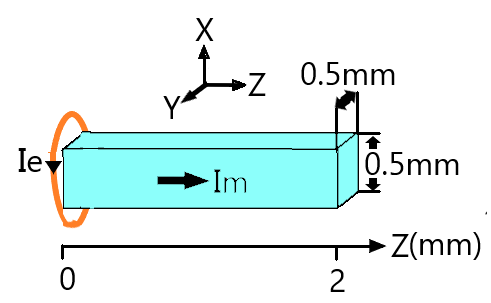


Figure : Geometry of Simulated Magnetic Transmission Line and Current Source

## Visualization of Electromagnetic Fields

The Longitudinal Fields of the simulated transmission line are shown in the table below.

|  |  |  |  |
| --- | --- | --- | --- |
|  | Component | | |
| Field | X | Y | Z |
| H | D:\New folder\MGTL\Thesis\Codes\Code43\Logitudinal\hz-000050.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Logitudinal\hx-000050.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Logitudinal\hy-000050.25.png |
| B | D:\New folder\MGTL\Thesis\Codes\Code43\Logitudinal\bz-000050.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Logitudinal\bx-000050.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Logitudinal\by-000050.25.png |
| E | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Logitudinal\ez-000004.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Logitudinal\ex-000025.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Logitudinal\ey-000026.25.png |
| D | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Logitudinal\dz-000004.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Logitudinal\dx-000025.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Logitudinal\dy-000026.25.png |

The magnetization field **H** is zero inside the magnetic transmission line due to high magnetic permeability of the ferromagnetic material. The longitudinal magnetic field **Hz** is very intense inside the transmission line. The intense longitudinal **Hx** field results due to magnetic flux leakage. The transverse **Ex**, **Ey, Dx** and **Dy** show that electric fields encircle the transmission line.

The Transverse Fields of the simulated transmission line are shown in the table below.

|  |  |  |  |
| --- | --- | --- | --- |
|  | Component | | |
| Field | X | Y | Z |
| H | D:\New folder\MGTL\Thesis\Codes\Code43\Transverse\hz-000050.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Transverse\hx-000050.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Transverse\hy-000050.25.png |
| B | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Transverse\bz-000050.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Transverse\bx-000038.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Transverse\by-000050.25.png |
| E | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Transverse\ez-000020.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Transverse\ex-000019.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Transverse\ey-000050.25.png |
| D | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Transverse\dz-000045.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code43\Transverse\dx-000040.25.png | D:\New folder\MGTL\Thesis\Codes\Code43\Transverse\dy-000050.25.png |

The magnetization field **H** is zero inside the magnetic transmission line due to high magnetic permeability of the ferromagnetic material. Intense Transverse **Hx** and **Hy** fields show that **H** field radiates out from the magnetic transmission line in straight paths. The Magnetic Flux Density **Bz** is mainly confined inside the transmission Line. **Bx** and **By** components result from the magnetic leakage flux. The transverse **Ex, Ey, Dx** and **Dy** show that electric fields encircle the transmission line.

## Dispersion Characteristics

The variation of Permeability with frequency is shown in the figure below.



Figure : Variation of relative Permeability with applied Magnetic Field

## Attenuation of Magnetic Field along the direction of propagation

The diagram below shows the decay of Magnetic Field along the length of the Magnetic path. The wave front of the axial Magnetic Field evolves over time, spreading across the length of the line. The field is plotted in logarithmic scale to show the decay of the wave front as it propagates. When the wave front hits the opposite end, it is reflected so the final profile approaches a standing wave of constant magnitude.

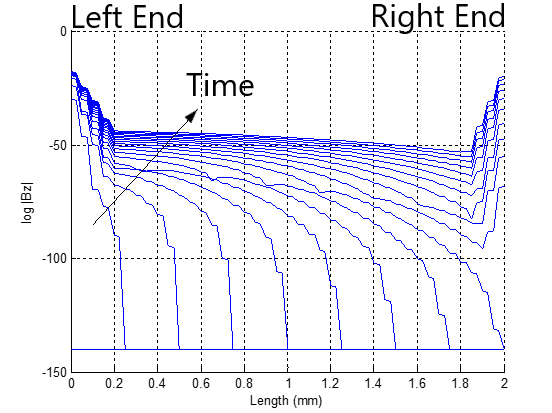
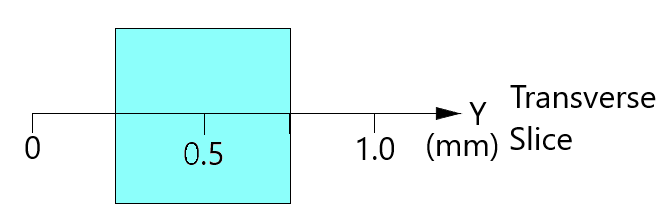


Figure : Evolution of pulse wave front across the length of the transmission line

## Skin Effect in Magnetic Transmission Line

The Electromagnetic fields decay very strongly inside the lossy transmission line due to skin effect.

****

The amplitudes of fields are plotted for a transverse slice of the ferromagnetic material in the figure below.



Figure : Decay of Electromagnetic Fields inside the lossy Magnetic Material

## Evolution of Magnetic displacement current and Voltage due to application of Gaussian Pulse



Figure : Evolution of Magnetic displacement current and Magnetic Voltage upon application of Gaussian Pulse

## Intrinsic Impedance of Magnetic Transmission Line



Figure : Variation of wave impedance magnitude and angle with frequency

At 1GHz,

At 10GHz,

## Attenuation Constant and Phase Constant of Magnetic Transmission Line



Figure : Variation of Attenuation Constant, Phase Constant and Phase Velocity with frequency

Beta(1e10)=13850 (10435 actual),

alpha(1e10)=583180 (7238 actual)

Sigma=5e-3\* 26.5415= 0.1327

## Magnetic Admittance of Magnetic Transmission Line



Figure : Variation of Magnetic Conductance, Magnetic Reluctance and Magnetic Capacitance with frequency

## Introduction to Wideband Transformers

Wideband Transformers are widely used in RF Electronics for voltage, current and impedance matching of unbalanced loads [35-36] [31] [29]. They provide DC isolation and common mode rejection for efficient AC transmission [67] [17] [14].

Wideband Transformers [29] provide impedance matching for interfacing different systems through accurate current and voltage transformation [35-36] [14]. The impedance transformation ratio is dictated by the square of the effective turns ratio between the primary and secondary side [31] [67].

Unlike an unbalanced network, a balanced network has none of its terminals connected to ground. It is difficult to interface balanced systems with unbalanced systems due to common mode currents [67] [31]. Balun transformer is used for providing DC isolation and maximum power transfer between a balanced and an unbalanced system. A Unun transformer is used for interfacing two unbalanced impedances, whereas a Balbal transformer connects two balanced systems [14].

Usually wideband transformers [29] are required in high frequency communication applications that require processing of small amounts of RF power in a wide frequency range [35-36] [17] [14] [31] [67]. For high power applications in Base Station Amplifiers, Repeaters, Satellites, Radar and VFDs, the power limitations of the core and winding must be controlled along with the parasitic losses [35-36] [65] [31] [20].

1. Telecommunication Applications: 4G, CDMA, EDGE, GSM, LMDS, LTE, MMDS, Handsets (Cellular, PHS, DECT, TV), Node B, Pagers, TD-SCDMA, TMA, UMTS, W-CDMA, Wi-Fi, WiMAX, Wireline (DSL, ADSL, DSLAM etc.), W-LAN, WLL.
2. Automotive Applications: IVHS, GPS, Tracking
3. Wireless Communication: Audio Systems, AMR, EPIRB, Marine Radar, Marine GPS, RFID Reader/ TAGS, Security Monitoring Systems, Radio Astronomy, Jammers.
4. STATCOM: DBS, LNBs, MODEMs, TMBs, V-SAT.
5. Medical Applications: CT, MR, Ultrasound, Telemetry.
6. Cable/ CATV and Broadband Fiber Communication: BPON, Cable (Set Top Box), Fiber Optic, FTTH, GPON, Hybrid Fiber Coax Network, MOCA.
7. Broadcast Applications: Radio, TV, LMDS.
8. Avionics: Radar, Surveillance Radar, MLS, TACAN, TCAS.

The performance of a wideband transformer [35-36] [29] [14] [17] can be analyzed by the following performance parameters:

1. Bandwidth [31]: The range of frequencies between the two maximum allowable attenuation (1 dB/ 2 dB/ 3 dB) points fmin and fmax. A high fractional bandwidth of 1000 or more can only be achieved if the primary and secondary windings are strongly coupled [29] [35-36] [67]. Besides attenuation, wideband transformer may also introduce undesirable phase noise in the system causing distortion of RF signal. The transformer must be designed to have a flat phase response in the desired frequency range [65] [31].
2. Insertion Loss: The ratio of power transfer between the source and an ideal load upon direct connection; and when the transformer is used for the connection. It is indicative of the power loss through the transformer under matched conditions [67] [35-36] [31]. For a typical wideband transformer, the insertion loss increases at low frequencies due to the low magnetizing reactance [29]. At high frequencies, the insertion loss increases due to the inter-winding capacitance and the leakage inductance [65] [29] [20]. Often, mid-band insertion loss (e.g. 0.5 dB) is taken as reference value [31] [67].
3. Return Loss: The ratio of applied power and reflected power due to impedance mismatch between the source and load [31]. Optimal impedance matching must maximize the return loss (e.g. 14 - 25 dB) over the entire operational bandwidth i.e. minimum input power must be reflected back to the source [35-36] [67] [65] [29].
4. Amplitude balance: The absolute difference in signal amplitude between the outputs of a center-tapped transformer [35-36] [67] [65] [29] [31].
5. Phase balance: The absolute difference in signal phase between the outputs of a center-tapped transformer [35-36] [67] [65] [29] [31].



Figure : Variation of Wideband Transformer Insertion Loss with frequency

## Electrical Circuit for Wideband Transformer

The equivalent electrical circuit diagram of a wideband transformer [35-36] [67] [31] [17] [14] is given below.



Figure : Electrical circuit for wideband transformer

represents the primary leakage inductance.

represents the secondary leakage inductance referred to the primary side.

represents the primary winding resistance.

represents the secondary winding resistance referred to the primary side.

is the shunt resistance representing core loss.

nM is the magnetizing inductance of the core.

is the shunt capacitance associated with the primary windings.

is the shunt capacitance associated with the secondary windings.

is the capacitance between the primary and secondary windings.

The operation of wideband transformer [29] [17] [14] can be divided into three distinct segments:

1. Low Frequency Region: The low frequency droop in the transfer characteristics is attributed to the diminishing shunt magnetizing reactance [67] [31] [29]. The loss can be reduced by inserting capacitance in series with the primary or secondary winding [65] [31] [35-36].
2. Mid-band Region: The parasitic inductances and capacitances can be ignored in the mid-band region [31]. The response is mainly effected by the series resistance of the windings and the shunt resistance of the core [67] [65] [35-36] [29].

1. High Frequency Region: The high frequency droop results from the losses in leakage inductances and shunt capacitances of the windings [31]. The reactance of leakage inductances increases greatly whereas the reactance of shunt capacitance decreases at high frequencies [67] [65] [29] [35-36].

## Magnetic Circuit for Wideband Transformer

The Magnetic circuit for the Wideband Transformer is shown below. It consists of a primary gyrator with gyration constant Np. The secondary side gyrator has a gyration constant of Ns.

The magnetic core is represented by a short transmission line section consisting of longitudinal Magnetic Capacitance CL which stores electric energy, longitudinal Magnetic Conductance GL which dissipated energy and Transverse Magnetic Inductance LT which stores magnetic energy.

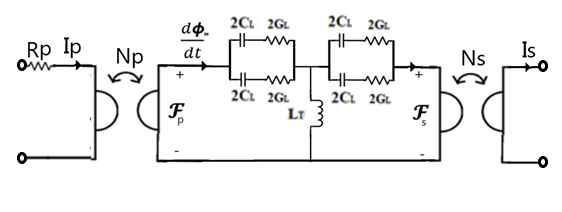


Figure :Magnetic circuit for wideband transformer based on small magnetic transmission line

## Simulation of Wideband Transformer in MEEP

The Magnetic Transmission Lines [22-26] will be constructed for inhomogeneous, dispersive [72] [16], non-linear [40] ferromagnetic substances [8] like nickel and Cobalt alloys. The Transmission Lines will be excited using continuous current sources. The terminations can be modeled by Perfectly matched layers for complete absorption; or as perfect reflectors for no load. Different Transmission Line structures can be simulated like shielded transmission line and multi-wire transmission lines.

A wideband transformer [29] [14] [17] passes a frequency band of several decades and are usually designed to handle complex waveforms like rectangular pulses [67] [59]. They are used for impedance matching, voltage/ current transformation, DC isolation, mixing, power splitting, coupling and signal inversion [65] [31]. The wideband transformer [14] [17] will be excited by a small Gaussian pulse to examine the Frequency Response [67] [59]. The 3 dimensional discrete Fourier Transform will be used to determine Transmittance and Broadband Response [67] [65] [59] [50] [17] [29] [31]. The results can be compared with published datasheet.

Figure : Outline of MEEP Algorithm for simulation of wideband transformer

## Visualization of Electromagnetic Fields

The Transverse Fields are shown in the table below.

|  |  |  |  |
| --- | --- | --- | --- |
|  | Component | | |
| Field | X | Y | Z |
| H | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\hx-001351.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\hy-001801.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\hz-002251.25.png |
| B | D:\New folder\MGTL\Thesis\Codes\Code46\MMTL-out\bx-005001.25.png | D:\New folder\MGTL\Thesis\Codes\Code46\MMTL-out\by-005001.25.png | D:\New folder\MGTL\Thesis\Codes\Code46\MMTL-out\bz-005001.25.png |
| E | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\ex-002726.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\ey-002726.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\ez-002726.25.png |
| D | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\dx-002726.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\dy-002726.25.png | D:\MuhammadShamaas\MGTL_Github\Thesis\Codes\Code46\MMTL-out\dz-002726.25.png |

## Calculating Bandwidth of Wideband Transformer using Frequency Response of Poynting Fluxes

The discrete Fourier Transform of the flux linkage of primary winding and secondary winding was used to determine the Insertion loss of the Wideband Transformer.



Figure : Input Poynting Flux, Output Poynting Flux and insetion loss of wideband transformer

# Conclusion

The conventional reluctance model is not accurate for the modeling of magnetic circuits [18]. It must be replaced by Magnetic Transmission Line Model [22-26] for accurate modeling of inhomogeneous, dispersive [72] [16], non-linear [40] [8] ferromagnetic structures.

The Loss tangent has the following components:

* DC Resistance Loss Tangent
* Skin Effect Loss Tangent
* Proximity Effect Loss Tangent
* Self Capacitance Dielectric Loss Tangent
* Self Capacitance Circulating Currents Loss Tangent
* Core Residual Loss Tangent
* Core Eddy Current Loss Tangent ,
* Core Hysteresis Loss Tangent ,

Non-linear [40] components must be used for these complex effects. Network Equivalent Magnetic circuits [18] and coupled equations will be used to simplify analysis of the transient [9] and steady state behavior.

* Magnetic coupling between magnetic transmission lines [22-26] results in sharing of electromagnetic energy. This division of power is very useful in design of Radio frequency devices like sensors [74] [66] [60], antennas and communication systems [14].
* Magnetic Coupling is also very important in the working of DC and AC machines like induction motor, hysteresis motor and Reluctance motor [11] [20].
* The study of capacitive/ inductive coupling in Multi-Conductor Transmission Lines will provide useful knowledge about the Radiated/ Conducted Emissions and Radiated/ Conducted Susceptibility.
* The results can be compared with MATLAB linear circuit models for cross talk between Magnetic Transmission Lines [22-26].
* The aim will be to minimize Electromagnetic Radiation; that can be picked up by unintentional receivers like digital Computers.

The simulators can not be used to model the following magnetic effects:

1. Magnetostriction
2. Accoustic effects
3. Relativistic Effects
4. Piezomagnetism
5. Gravitomagnetism

The power invariant Magnetic Transmission Line model [22-26] can also be used for accurate modeling of

* AC and DC Machines [20]
* Micro-strip Antennas
* Gyromagnetic NLTLs [71] [62] [61] [54]
* Magnetic Transistors and Magnetic Microprocessors

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# Appendix

## MEEP Code

#include <iostream>

#include <fstream>

#include <stdio.h>

#include <stdlib.h>

#include <string.h>

#include <complex>

#include "meep.hpp"

#include "ctl-math.h"

#include <mpb.h>

#include "ctlgeom.h"

#include "meepgeom.hpp"

#include <math.h>

#ifndef DATADIR

#define DATADIR "./"

#endif

using namespace meep;

using namespace std;

typedef std::complex<double> cdouble;

double epsr=0.9999;

//SI Conversion Factors

double a0=1e-4;//0.1mm

double c0=2.99792458e8;//Speed of Light (m/s)

double f0=c0/a0;//300GHz

double t0=1/f0;//0.33e-11 (s)

double mu0=4\*pi\*(1e-7);// (H/m)

double eps0=8.854187817e-12;// (F/m)

double I0=1; //(A)

double E0=I0/(a0\*eps0\*c0);//Electric Field

double D0=I0/(a0\*c0);//Electric Displacement Field

double B0=I0/(a0\*eps0\*c0\*c0);//Magnetic Field

double H0=I0/(a0);//Magnetizing Field

double sigmaD0=(epsr\*eps0\*c0)/a0;//Electric Conductivity

double J0=I0/(a0\*a0);//Electric Current Density

double u0=(I0\*I0)/(eps0\*c0\*c0\*a0\*a0);//Energy Density

double S0=(I0\*I0)/(eps0\*c0\*a0\*a0);//Poynting Vector

double Sc0=1/(c0);//Courant Factor

double xcen=0.0, ycen=0.0, zcen=0.0;

double dxmin=0.0, dxmax=02.5, dymin=0.0, dymax=02.5, dzmin=0.0, dzmax=10.0;

double wcore=2.0\*dymax;

double winding\_thickness\_p=01.0, insulation\_thickness\_p=02.5,pml\_thickness=1.0;

//double sigma\_Cu=100000000;

double mu\_core=10000;

int Np=1;//must be odd

int Ns=1;//must be odd

double margin=02.0;

double amplitude=1.0;

double divisions=2;

int numcoord=0;

int corecoord=0;

double k=2\*pi\*Np/(2\*dzmin);

double theta=0.0;

double rp=(wcore/2.0)+(winding\_thickness\_p/2.0)+insulation\_thickness\_p;

double \* xpcoord=new double [1000000];

double \* ypcoord=new double [1000000];

double \* zpcoord=new double [1000000];

double \* xscoord=new double [1000000];

double \* yscoord=new double [1000000];

double \* zscoord=new double [1000000];

double \* xccoord=new double [1000000];

double \* yccoord=new double [1000000];

double \* zccoord=new double [1000000];

//Copper

//metal\_range = mp.FreqRange(min=um\_scale/12.398, max=um\_scale/.20664)

double um\_scale = 100.0;//100um

double eV\_um\_scale = 1.0/1.23984193;

double Cu\_plasma\_frq = 10.83\*eV\_um\_scale;

double Cu\_f0 = 0.575;

double Cu\_frq0 = 1e-10;

double Cu\_gam0 = 0.030\*eV\_um\_scale;

double Cu\_sig0 = Cu\_f0\*(Cu\_plasma\_frq\*Cu\_plasma\_frq)/(Cu\_frq0\*Cu\_frq0);

double Cu\_f1 = 0.061;

double Cu\_frq1 = 0.291\*eV\_um\_scale;

double Cu\_gam1 = 0.378\*eV\_um\_scale;

double Cu\_sig1 = Cu\_f1\*(Cu\_plasma\_frq\*Cu\_plasma\_frq)/(Cu\_frq1\*Cu\_frq1);

double Cu\_f2 = 0.104;

double Cu\_frq2 = 2.957\*eV\_um\_scale;

double Cu\_gam2 = 1.056\*eV\_um\_scale;

double Cu\_sig2 = Cu\_f2\*(Cu\_plasma\_frq\*Cu\_plasma\_frq)/(Cu\_frq2\*Cu\_frq2);

double Cu\_f3 = 0.723;

double Cu\_frq3 = 5.300\*eV\_um\_scale;

double Cu\_gam3 = 3.213\*eV\_um\_scale;

double Cu\_sig3 = Cu\_f3\*(Cu\_plasma\_frq\*Cu\_plasma\_frq)/(Cu\_frq3\*Cu\_frq3);

double Cu\_f4 = 0.638;

double Cu\_frq4 = 11.18\*eV\_um\_scale;

double Cu\_gam4 = 4.305\*eV\_um\_scale;

double Cu\_sig4 = Cu\_f4\*(Cu\_plasma\_frq\*Cu\_plasma\_frq)/(Cu\_frq4\*Cu\_frq4);

double sigma\_Cu=Cu\_sig0;

//NiFe

//NiFe\_range = mp.FreqRange(min=um\_scale/0.83, max=um\_scale/0.25)

double NiFe\_frq = 1/(0.0838297450980392\*um\_scale);

double NiFe\_gam = 1/(0.259381156903766\*um\_scale);

double NiFe\_sig = 1;

double annulus(const vec & v, double xcen, double ycen, double zcen, double dxmin, double dxmax, double dymin, double dymax, double dzmin, double dzmax, double control, double special, double std = 0.0)

{

double mu=control;

double dx=v.x() - xcen;

double dy=v.y() - ycen;

double dz=v.z() - zcen;

if ( (abs(dx)<=dxmax) && (abs(dy)<=dymax) && (abs(dz)<=dzmax) )

{

{mu= gaussian\_random(special,std);}

}

if ( (abs(dx)<=dxmin) && (abs(dy)<=dymin) && (abs(dz)<=dzmin) )

{

mu= control;

}

return mu;

}

bool inside\_box(const vec & v, double xcen, double ycen, double zcen, double dxmax, double dymax, double dzmax)

{

bool ans=false;

double dx=v.x() - xcen;

double dy=v.y() - ycen;

double dz=v.z() - zcen;

if ( (abs(dx)<=dxmax) && (abs(dy)<=dymax) && (abs(dz)<=dzmax) )

{

{ans=true;}

}

return ans;

}

cdouble line\_integral\_x(fields & f, component C, double dx, double xmin, double xmax, double y, double z)

{

cdouble sum(0.0,0.0);

cdouble deltax(dx,0.0);

for (double x=xmin; x<=xmax; x=x+dx)

{

monitor\_point p;

f.get\_point(&p, vec(x,y,z));

cdouble dF = p.get\_component(C);

sum += dF\*deltax;

}

return sum;

}

cdouble line\_integral\_y(fields & f, component C, double dy, double ymin, double ymax, double x, double z)

{

cdouble sum(0.0,0.0);

cdouble deltay(dy,0.0);

for (double y=ymin; y<=ymax; y=y+dy)

{

monitor\_point p;

f.get\_point(&p, vec(x,y,z));

cdouble dF = p.get\_component(C);

sum += dF\*deltay;

}

return sum;

}

cdouble line\_integral\_z(fields & f, component C, double dz, double zmin, double zmax, double x, double y)

{

cdouble sum(0.0,0.0);

cdouble deltaz(dz,0.0);

for (double z=zmin; z<=zmax; z=z+dz)

{

monitor\_point p;

f.get\_point(&p, vec(x,y,z));

cdouble dF = p.get\_component(C);

//cout<<dF.real()<<" , "<<dF.imag()<<endl;

sum += dF\*deltaz;

//cout<<dF.real()<<" , "<<dF.imag()<<endl;

}

return sum;

}

cdouble compute\_Im(fields & f, double z)

{

cdouble Iyf=line\_integral\_y(f,Ey,0.001,ycen-dymax,ycen+dymax,xcen+dxmax,z);

cdouble Iyb=line\_integral\_y(f,Ey,0.001,ycen-dymax,ycen+dymax,xcen-dxmax,z);

cdouble Ixt=line\_integral\_x(f,Ex,0.001,xcen-dxmax,xcen+dxmax,ycen-dymax,z);

cdouble Ixb=line\_integral\_x(f,Ex,0.001,xcen-dxmax,xcen+dxmax,ycen+dymax,z);

cdouble Im=Ixt+Iyf-Ixb-Iyb;

return Im;

}

cdouble compute\_Ie(fields & f, double z)

{

cdouble Iyf=line\_integral\_y(f,Hy,0.001,ycen-dymax,ycen+dymax,xcen+dxmax,z);

cdouble Iyb=line\_integral\_y(f,Hy,0.001,ycen-dymax,ycen+dymax,xcen-dxmax,z);

cdouble Ixt=line\_integral\_x(f,Hx,0.001,xcen-dxmax,xcen+dxmax,ycen-dymax,z);

cdouble Ixb=line\_integral\_x(f,Hx,0.001,xcen-dxmax,xcen+dxmax,ycen+dymax,z);

cdouble Ie=Ixt+Iyf-Ixb-Iyb;

return Ie;

}

cdouble compute\_Vm(fields & f, double z)

{

//cdouble Vy=line\_integral\_y(f,Hy,0.001,ycen-dymin,y,xcen,zcen-dzmin);

cdouble Vz=line\_integral\_z(f,Hz,0.001,zcen-dzmax,z,xcen,ycen);

//cdouble Vm=Vy+Vz;

return Vz;

}

cdouble compute\_Ve(fields & f, double z)

{

//cdouble Vy=line\_integral\_y(f,Ey,0.001,ycen-dymin,y,xcen,zcen-dzmin);

cdouble Vz=line\_integral\_z(f,Ez,0.001,zcen-dzmax,z,xcen,ycen);

//cdouble Ve=Vy+Vz;

return Vz;

}

double mu(const vec &v)

{

//return annulus(v,xcen,ycen,zcen,dxmin,dxmax,dymin,dymax,dzmin,dzmax,1.0,mu\_core,0.0);

return 1.0;

}

double eps(const vec &v)

{

//return annulus(v,xcen,ycen,zcen,dxmin,dxmax,dymin,dymax,dzmin,dzmax,1.0,3.5,0.0);

return 1.0;

}

double conductivity(const vec &v)

{

}

class core\_material : public material\_function {

public:

};

class winding\_material : public material\_function {

public:

};

typedef struct my\_material\_func\_data {

double rxInner, ryInner, rOuter;

bool with\_susceptibility;

} my\_material\_func\_data;

void my\_material\_func(vector3 p, void \*user\_data, meep\_geom::medium\_struct \*m) {

my\_material\_func\_data \*data = (my\_material\_func\_data \*)user\_data;

bool in\_middle=false;

double dx=p.x - xcen;

double dy=p.y - ycen;

double dz=p.z - zcen;

for (int i=0; i<corecoord; i++) {

double dxp=p.x - xccoord[i];

double dyp=p.y - yccoord[i];

double dzp=p.z - zccoord[i];

double drp=sqrt(dxp\*dxp+dyp\*dyp+dzp\*dzp);

if((dxp<=(wcore/2.0))&&(dyp<=(wcore/2.0))&&(dzp<=(wcore/2.0))){

in\_middle=true;

}

}

// set permittivity and permeability

double nn = in\_middle ? sqrt(mu\_core) : 1.0;

double mm = in\_middle ? sqrt(10.0) : 1.0;

m->epsilon\_diag.x = m->epsilon\_diag.y = m->epsilon\_diag.z = mm \* mm;

//m->epsilon\_offdiag.x.re = m->epsilon\_offdiag.x.im = epsilon\_offdiag.y.re = m->epsilon\_offdiag.y.im = epsilon\_offdiag.z.re = m->epsilon\_offdiag.z.im = nn \* nn;

m->mu\_diag.x = m->mu\_diag.y = m->mu\_diag.z = nn\*nn;

//m->mu\_offdiag.x.re = m->mu\_offdiag.x.im = mu\_offdiag.y.re = m->mu\_offdiag.y.im = mu\_offdiag.z.re = m->mu\_offdiag.z.im = nn \* nn;

m->E\_chi2\_diag.x = m->E\_chi2\_diag.y = m->E\_chi2\_diag.z = 1.0;

m->E\_chi3\_diag.x = m->E\_chi3\_diag.y = m->E\_chi3\_diag.z = 1.0;

m->H\_chi2\_diag.x = m->H\_chi2\_diag.y = m->H\_chi2\_diag.z = 1.0;

m->H\_chi3\_diag.x = m->H\_chi3\_diag.y = m->H\_chi3\_diag.z = 1.0;

//m->D\_conductivity\_diag.x = m->D\_conductivity\_diag.y = m->D\_conductivity\_diag.z = nn \* nn;

//m->B\_conductivity\_diag.x = m->B\_conductivity\_diag.y = m->B\_conductivity\_diag.z = 0.0;

if (in\_middle)

{

m->H\_susceptibilities.num\_items = 1;

m->H\_susceptibilities.items = new meep\_geom::susceptibility[1];

m->H\_susceptibilities.items[0].sigma\_offdiag.x = 0.0;

m->H\_susceptibilities.items[0].sigma\_offdiag.y = 0.0;

m->H\_susceptibilities.items[0].sigma\_offdiag.z = 0.0;

m->H\_susceptibilities.items[0].sigma\_diag.x = gaussian\_random(1.0,1.0);//NiFe\_sig;

m->H\_susceptibilities.items[0].sigma\_diag.y = gaussian\_random(1.0,1.0);//NiFe\_sig;

m->H\_susceptibilities.items[0].sigma\_diag.z = gaussian\_random(1.0,1.0);//NiFe\_sig;

m->H\_susceptibilities.items[0].bias.x = gaussian\_random(1.0,1.0);

m->H\_susceptibilities.items[0].bias.y = gaussian\_random(1.0,1.0);

m->H\_susceptibilities.items[0].bias.z = gaussian\_random(1.0,1.0);

m->H\_susceptibilities.items[0].frequency = (0.2e6)/f0;//NiFe\_frq;

m->H\_susceptibilities.items[0].gamma = 100.0\*((0.2e6)/f0);//NiFe\_gam;

m->H\_susceptibilities.items[0].alpha = gaussian\_random(1.0,1.0);//NiFe\_alpha;

m->H\_susceptibilities.items[0].noise\_amp = 0.01;

m->H\_susceptibilities.items[0].drude = false;

m->H\_susceptibilities.items[0].saturated\_gyrotropy = true;

m->H\_susceptibilities.items[0].is\_file = false;

m->D\_conductivity\_diag.x = m->D\_conductivity\_diag.y = m->D\_conductivity\_diag.z = (5e-3)/sigmaD0;

}

for (int i=0; i<numcoord; i++) {

double dxp=p.x - xpcoord[i];

double dyp=p.y - ypcoord[i];

double dzp=p.z - zpcoord[i];

double drp=sqrt(dxp\*dxp+dyp\*dyp+dzp\*dzp);

if(drp<=(winding\_thickness\_p/2.0)){

m->D\_conductivity\_diag.x = m->D\_conductivity\_diag.y = m->D\_conductivity\_diag.z = 5.8e7/sigmaD0;

}

double dxs=p.x - xscoord[i];

double dys=p.y - yscoord[i];

double dzs=p.z - zscoord[i];

double drs=sqrt(dxs\*dxs+dys\*dys+dzs\*dzs);

if(drs<=(winding\_thickness\_p/2.0)){

m->D\_conductivity\_diag.x = m->D\_conductivity\_diag.y = m->D\_conductivity\_diag.z = 5.8e7/sigmaD0;

}

}

if ( (p.z<(zcen-dzmax))||(p.z>(zcen+dzmax)) ) {

//m->D\_conductivity\_diag.x = m->D\_conductivity\_diag.y = m->D\_conductivity\_diag.z = 1e20;

//m->B\_conductivity\_diag.x = m->B\_conductivity\_diag.y = m->B\_conductivity\_diag.z = 1e20;

//m->epsilon\_diag.x = m->epsilon\_diag.y = m->epsilon\_diag.z = 20.0;

//m->mu\_diag.x = m->mu\_diag.y = m->mu\_diag.z = 1e20;

}

}

int main(int argc, char \*argv[]) {

initialize mpi(argc,argv);

const char \*mydirname = "MMTL-out";

std::ofstream Time;

std::ofstream Space;

std::ofstream FieldsIn;

std::ofstream FieldsOut;

std::ofstream Fluxes;

std::ofstream Skin;

Time.open ("TimeEvolution.txt");

Space.open ("SpaceEvolution.txt");

FieldsIn.open ("FieldEvolutionIn.txt");

FieldsOut.open ("FieldEvolutionOut.txt");

Fluxes.open ("Flux.txt");

Skin.open ("Skin.txt");

//trash\_output\_directory(mydirname);

double xsize=10;

double ysize=50;

double zsize=50;

//double xsize=6, ysize=6, zsize=6;

k=2\*pi\*Np/(03.0);

for (double z = -04.0; z <= -1.0; z=z+0.1)

{

theta=k\*(z+04.0);

xpcoord[numcoord]=-rp\*sin(theta);

ypcoord[numcoord]=rp\*cos(theta);

zpcoord[numcoord]=z;

xscoord[numcoord]=-rp\*sin(theta);

yscoord[numcoord]=rp\*cos(theta);;

zscoord[numcoord]=z+05.0;

numcoord++;

}

for(double y=-12.5;y<=12.5;y=y+12.5)

{for (double z=-07.5;z<=07.5;z=z+00.1){

xccoord[corecoord]=xcen;

yccoord[corecoord]=y;

zccoord[corecoord]=z;

corecoord++;

}}

for(double z=-07.5;z<=07.5;z=z+15.0)

{for (double y=-12.5;y<=12.5;y=y+00.1){

xccoord[corecoord]=xcen;

yccoord[corecoord]=y;

zccoord[corecoord]=z;

corecoord++;

}}

grid\_volume gv = vol3d(xsize, ysize, zsize, divisions);

//grid\_volume vol3d(double xsize, double ysize, double zsize, double a);

gv.center\_origin();

//void center\_origin(void) { shift\_origin(-icenter()); }

structure transformer(gv, eps, pml(pml\_thickness));

//transformer.set\_epsilon(eps,true);

//transformer.set\_mu(mu,true);

//transformer.add\_susceptibility(core\_mat, H\_stuff, lorentzian\_susceptibility(2\*pi\*NiFe\_frq, NiFe\_gam, true));

//transformer.add\_susceptibility(core\_mat, H\_stuff, gyrotropic\_susceptibility(vec(0.0,0.0,0.0),2\*pi\*NiFe\_frq, NiFe\_gam, true));

//gyrotropic\_susceptibility(const vec &bias, double omega\_0, double gamma, double alpha = 0.0,gyrotropy\_model model = GYROTROPIC\_LORENTZIAN);

transformer.set\_output\_directory(mydirname);

//transformer->set\_chi2(mu);

//transformer->set\_chi3(mu);

meep\_geom::medium\_struct my\_medium\_struct;

my\_medium\_struct.epsilon\_diag.x = 1.0;

my\_medium\_struct.epsilon\_diag.y = 1.0;

my\_medium\_struct.epsilon\_diag.z = 1.0;

my\_medium\_struct.mu\_diag.x=1.0;

my\_medium\_struct.mu\_diag.y=1.0;

my\_medium\_struct.mu\_diag.z=1.0;

/\*my\_medium\_struct.mu\_offdiag.x=mu\_core;

my\_medium\_struct.mu\_offdiag.y=mu\_core;

my\_medium\_struct.mu\_offdiag.z=mu\_core;

\*/my\_medium\_struct.H\_chi2\_diag.x=1.0;

my\_medium\_struct.H\_chi2\_diag.y=1.0;

my\_medium\_struct.H\_chi2\_diag.z=1.0;

my\_medium\_struct.H\_chi3\_diag.x=1.0;

my\_medium\_struct.H\_chi3\_diag.y=1.0;

my\_medium\_struct.H\_chi3\_diag.z=1.0;

my\_medium\_struct.E\_chi2\_diag.x=1.0;

my\_medium\_struct.E\_chi2\_diag.y=1.0;

my\_medium\_struct.E\_chi2\_diag.z=1.0;

my\_medium\_struct.E\_chi3\_diag.x=1.0;

my\_medium\_struct.E\_chi3\_diag.y=1.0;

my\_medium\_struct.E\_chi3\_diag.z=1.0;

//m->epsilon\_offdiag.x.re = m->epsilon\_offdiag.x.im = epsilon\_offdiag.y.re = m->epsilon\_offdiag.y.im = epsilon\_offdiag.z.re = m->epsilon\_offdiag.z.im = nn \* nn;

//m->mu\_offdiag.x.re = m->mu\_offdiag.x.im = mu\_offdiag.y.re = m->mu\_offdiag.y.im = mu\_offdiag.z.re = m->mu\_offdiag.z.im = nn \* nn;

//m->E\_chi2\_diag.x = m->E\_chi2\_diag.y = m->E\_chi2\_diag.z = mu\_core;

//m->E\_chi3\_diag.x = m->E\_chi3\_diag.y = m->E\_chi3\_diag.z = mu\_core;

//m->H\_chi2\_diag.x = m->H\_chi2\_diag.y = m->H\_chi2\_diag.z = mu\_core;

//m->H\_chi3\_diag.x = m->H\_chi3\_diag.y = m->H\_chi3\_diag.z = mu\_core;

//m->D\_conductivity\_diag.x = m->D\_conductivity\_diag.y = m->D\_conductivity\_diag.z = nn \* nn;

//m->B\_conductivity\_diag.x = m->B\_conductivity\_diag.y = m->B\_conductivity\_diag.z = 0.0;

my\_medium\_struct.H\_susceptibilities.num\_items = 1;

my\_medium\_struct.H\_susceptibilities.items = new meep\_geom::susceptibility[1];

my\_medium\_struct.H\_susceptibilities.items[0].sigma\_offdiag.x = 0.0;

my\_medium\_struct.H\_susceptibilities.items[0].sigma\_offdiag.y = 0.0;

my\_medium\_struct.H\_susceptibilities.items[0].sigma\_offdiag.z = 0.0;

my\_medium\_struct.H\_susceptibilities.items[0].sigma\_diag.x = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].sigma\_diag.y = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].sigma\_diag.z = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].bias.x = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].bias.y = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].bias.z = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].frequency = (0.2e6/f0);

my\_medium\_struct.H\_susceptibilities.items[0].gamma = 100.0\*(0.2e6/f0);

my\_medium\_struct.H\_susceptibilities.items[0].alpha = gaussian\_random(1.0,1.0);

my\_medium\_struct.H\_susceptibilities.items[0].noise\_amp = 0.01;

my\_medium\_struct.H\_susceptibilities.items[0].drude = false;

my\_medium\_struct.H\_susceptibilities.items[0].saturated\_gyrotropy = true;

my\_medium\_struct.H\_susceptibilities.items[0].is\_file = false;

my\_material\_func\_data data;

data.with\_susceptibility = true;

meep\_geom::material\_type default\_material =meep\_geom::make\_dielectric(1.0);

//default\_material->which\_subclass = material\_data::MEDIUM;

default\_material->medium=my\_medium\_struct;

default\_material->user\_func = my\_material\_func;

default\_material->user\_data = (void \*) &data;

default\_material->do\_averaging = false;

meep\_geom::material\_type my\_user\_material =meep\_geom::make\_user\_material(my\_material\_func, (void \*)&data, false);

//vector3 center = {0, 0, 0};

//geometric\_object go = ctlgeom::geometric\_object(my\_material,center);

geometric\_object objects[5];

vector3 center = {0.0, 0.0, 0.0};

vector3 center1 = {0.0, -12.5, 0.0};

vector3 center2 = {0.0, 0.0, 0.0};

vector3 center3 = {0.0, 12.5, 0.0};

vector3 center4 = {0.0, 0.0, 07.5};

vector3 center5 = {0.0, 0.0, -07.5};

double radius = 3.0;

double height = 1.0e20;

vector3 xhat1 = {1.0, 0.0, 0.0};

vector3 yhat1 = {0.0, 1.0, 0.0};

vector3 zhat1 = {0.0, 0.0, 1.0};

vector3 size1 = {wcore, wcore, 20.0};

vector3 size2 = {wcore, wcore, 20.0};

vector3 size3 = {wcore, wcore, 20.0};

vector3 size4 = {wcore, 30.0, wcore};

vector3 size5 = {wcore, 30.0, wcore};

//objects[0] = make\_block(my\_material, center, radius, height, zhat);

objects[0] = make\_block(my\_user\_material, center1, xhat1, yhat1, zhat1, size1);

objects[1] = make\_block(my\_user\_material, center2, xhat1, yhat1, zhat1, size2);

objects[2] = make\_block(my\_user\_material, center3, xhat1, yhat1, zhat1, size3);

objects[3] = make\_block(my\_user\_material, center4, xhat1, yhat1, zhat1, size4);

objects[4] = make\_block(my\_user\_material, center5, xhat1, yhat1, zhat1, size5);

geometric\_object\_list g = {5, objects};

//geometric\_object\_list g = {0,0};

//g.num\_items=1;

meep\_geom::absorber\_list al= new meep\_geom::absorber\_list\_type;

meep\_geom::material\_type\_list mtl= meep\_geom::material\_type\_list();

mtl.num\_items=1;

mtl.items=new meep\_geom::material\_type;

mtl.items[0]=my\_user\_material;

cout<<"MAIN "<<mtl.num\_items<<endl;

bool use\_anisotropic\_averaging = false;

bool ensure\_periodicity = true;

set\_materials\_from\_geometry(&transformer, g, center, use\_anisotropic\_averaging,DEFAULT\_SUBPIXEL\_TOL, DEFAULT\_SUBPIXEL\_MAXEVAL,ensure\_periodicity, default\_material,al,mtl);

/\*

winding\_material winding\_mat;

structure winding(gv, winding\_mat);

//winding.set\_epsilon(eps);

winding.set\_conductivity(Ex,conductivity);

winding.set\_conductivity(Ey,conductivity);

winding.set\_conductivity(Ez,conductivity);

winding.add\_susceptibility(winding\_mat, E\_stuff, lorentzian\_susceptibility(2\*pi\*Cu\_frq0, Cu\_gam0, true));

winding.add\_susceptibility(winding\_mat, E\_stuff, lorentzian\_susceptibility(2\*pi\*Cu\_frq1, Cu\_gam1));

winding.add\_susceptibility(winding\_mat, E\_stuff, lorentzian\_susceptibility(2\*pi\*Cu\_frq2, Cu\_gam2));

winding.add\_susceptibility(winding\_mat, E\_stuff, lorentzian\_susceptibility(2\*pi\*Cu\_frq3, Cu\_gam3));

winding.add\_susceptibility(winding\_mat, E\_stuff, lorentzian\_susceptibility(2\*pi\*Cu\_frq4, Cu\_gam4));

//lorentzian\_susceptibility(double omega\_0, double gamma, bool no\_omega\_0\_denominator = false): omega\_0(omega\_0), gamma(gamma), no\_omega\_0\_denominator(no\_omega\_0\_denominator)

\*/

fields f(& transformer);

//fields(structure \*, double m = 0, double beta = 0, bool zero\_fields\_near\_cylorigin = true);

for (double fp=0.0;fp<=3.0\*(1e9/f0);fp=fp+0.5\*(1e9/f0))

{ cout<<fp<<endl;

for (double yp = -20.0; yp <= 20.0; yp=yp+10.0)

{

cout<<f.get\_mu(vec(0.0,yp,(dzmin+dzmax)/2.0),fp)-10000<<" ";

}

cout<<endl;

}

double xcenp=xcen;

double ycenp=ycen-dymin-(0.5\*wcore);

double zcenp=zcen;

double dxminp=dxmax+insulation\_thickness\_p;

double dxmaxp=dxminp+winding\_thickness\_p;

double dyminp=(0.5\*wcore)+insulation\_thickness\_p;

double dymaxp=dyminp+winding\_thickness\_p;

double dzminp=0;

double dzmaxp=0.5\*winding\_thickness\_p;

zcenp=zcen-(0.5\*double(Np-1)\*insulation\_thickness\_p)-(0.5\*double(Np-1)\*winding\_thickness\_p);

/\*for (int i=0;i<Np;i++)

{

const volume vsrc1 =volume(vec(xcenp+dxmaxp,ycenp-dymaxp,zcenp+dzmaxp), vec(xcenp+dxminp,ycenp+dymaxp,zcenp-dzmaxp));

const volume vsrc2 =volume(vec(xcenp+dxmaxp,ycenp+dymaxp,zcenp+dzmaxp), vec(xcenp-dxmaxp,ycenp+dyminp,zcenp-dzmaxp));

const volume vsrc3 =volume(vec(xcenp-dxmaxp,ycenp+dymaxp,zcenp+dzmaxp), vec(xcenp-dxminp,ycenp-dymaxp,zcenp-dzmaxp));

const volume vsrc4 =volume(vec(xcenp-dxmaxp,ycenp-dyminp,zcenp+dzmaxp), vec(xcenp+dxmaxp,ycenp-dymaxp,zcenp-dzmaxp));

f.add\_volume\_source(Ey, src, vsrc1, cdouble(amplitude,0));

f.add\_volume\_source(Ex, src, vsrc2, cdouble(-amplitude,0));

f.add\_volume\_source(Ey, src, vsrc3, cdouble(-amplitude,0));

f.add\_volume\_source(Ex, src, vsrc4, cdouble(amplitude,0));

zcenp=zcenp+insulation\_thickness\_p+winding\_thickness\_p;

}\*/

//f\_range;1e-5,1e-2

double fcen = (1e10)/f0; // ; pulse center frequency

double df = 0.999999\*((1e10)/f0); // ; df

//continuous\_src\_time src(cdouble(fcen,0));

//gaussian\_src\_time src(fcen,df);

for (int i=0;i<numcoord;i++)

{

theta=k\*(zpcoord[i]+05.0);

const volume vsrc1 =volume(vec(xpcoord[i],ypcoord[i],zpcoord[i]), vec(xpcoord[i],ypcoord[i],zpcoord[i]));

//for (double fr = 100000000.0; fr <= 1000000000.0; fr=fr+100000000.0)

{

//continuous\_src\_time src(cdouble(fr/f0,0.0));

gaussian\_src\_time src(fcen,df);

f.add\_volume\_source(Ex, src, vsrc1, cdouble(amplitude\*cos(theta),0));

f.add\_volume\_source(Ey, src, vsrc1, cdouble(-amplitude\*sin(theta),0));

}

}

//void add\_point\_source(component c, double freq, double width, double peaktime, double cutoff, const vec &, std::complex<double> amp = 1.0, int is\_continuous = 0);

//void add\_volume\_source(component c, const src\_time &src, const volume &, std::complex<double> amp = 1.0);

xcenp=xcen;

ycenp=ycen-dymin-(05.0\*wcore);

zcenp=zcen;

volume box1( vec(dxmax,-dymax,-05.0), vec(-dxmax,dymax,0.0) );

ycenp=ycen+dymin+(0.5\*wcore);

volume box2( vec(dxmax,-dymax,0.0), vec(-dxmax,dymax,05.0) );

fcen = (1e10)/f0; // ; pulse center frequency

df = 0.001\*(fcen/f0); // ; df

double fmin = 0, fmax = (1e11)/f0;

int Nfreq = 1000;

dft\_flux flux1 = f.add\_dft\_flux\_box(box1, fmin, fmax, Nfreq);

dft\_flux flux2 = f.add\_dft\_flux\_box(box2, fmin, fmax, Nfreq);

double init\_energy = f.field\_energy\_in\_box(box1);

/\*vec lb(vec()), rb(vec());

vec lt(vec()), rt(vec());

flux\_vol \*left = f.add\_flux\_plane(lb, lt);

flux\_vol \*right = f.add\_flux\_plane(rb, rt);

flux\_vol \*bottom = f.add\_flux\_plane(lb, rb);

flux\_vol \*top = f.add\_flux\_plane(lt, rt);

long double fluxL = 0;

\*/

//integral of flux = change in energy of box

f.step();

f.step();

f.step();

f.step();

f.step();

cout<<"Okay"<<endl;

volume vxy=volume(vec(-xsize+10,-ysize+10,0),vec(xsize-10,ysize-10,0));

volume vxz=volume(vec(-xsize+10,0,-zsize+10),vec(xsize-10,0,zsize-10));

volume vyz=volume(vec(0,-ysize+10,-zsize+10),vec(0,ysize-10,zsize-10));

/\*h5file \* fEx=f.open\_h5file("fEx",h5file::WRITE,0,false);

h5file \* fEy=f.open\_h5file("fEy",h5file::WRITE,0,false);

h5file \* fEz=f.open\_h5file("fEz",h5file::WRITE,0,false);

h5file \* fDx=f.open\_h5file("fDx",h5file::WRITE,0,false);

h5file \* fDy=f.open\_h5file("fDy",h5file::WRITE,0,false);

h5file \* fDz=f.open\_h5file("fDz",h5file::WRITE,0,false);

h5file \* fHx=f.open\_h5file("fHx",h5file::WRITE,0,false);

h5file \* fHy=f.open\_h5file("fHy",h5file::WRITE,0,false);

h5file \* fHz=f.open\_h5file("fHz",h5file::WRITE,0,false);

h5file \* fBx=f.open\_h5file("fBx",h5file::WRITE,0,false);

h5file \* fBy=f.open\_h5file("fBy",h5file::WRITE,0,false);

h5file \* fBz=f.open\_h5file("fBz",h5file::WRITE,0,false);

f.output\_hdf5(Dielectric,vyz,fEx);

f.output\_hdf5(Permeability,vyz,fEy);

f.output\_hdf5(Ez,vyz,fEz);

f.output\_hdf5(Dx,vyz,fDx);

f.output\_hdf5(Dy,vyz,fDy);

f.output\_hdf5(Dz,vyz,fDz);

f.output\_hdf5(Hx,vyz,fHx);

f.output\_hdf5(Hy,vyz,fHy);

f.output\_hdf5(Hz,vyz,fHz);

f.output\_hdf5(Bx,vyz,fBx);

f.output\_hdf5(By,vyz,fBy);

f.output\_hdf5(Bz,vyz,fBz);\*/

int stop=0;

for(int i=1;i<=1000000;i++)

{

if(!stop)

{f.step();}

if (stop)

{

i=1000001;

}

//fluxL += f.dt \* (left->flux() - right->flux() + bottom->flux() - top->flux());

if ((i%100)==0)

{

f.output\_hdf5(Hx,vyz);

f.output\_hdf5(Hy,vyz);

f.output\_hdf5(Hz,vyz);

f.output\_hdf5(Bx,vyz);

f.output\_hdf5(By,vyz);

f.output\_hdf5(Bz,vyz);

f.output\_hdf5(Ex,vyz);

f.output\_hdf5(Ey,vyz);

f.output\_hdf5(Ez,vyz);

f.output\_hdf5(Dx,vyz);

f.output\_hdf5(Dy,vyz);

f.output\_hdf5(Dz,vyz);

f.output\_hdf5(Sx,vyz);

f.output\_hdf5(Sy,vyz);

f.output\_hdf5(Sz,vyz);

}

if ((i%100)==0)

{

cdouble Vm=compute\_Vm(f,ycen);

cdouble Im=compute\_Im(f,ycen);

cdouble Ve=compute\_Ve(f,ycen);

cdouble Ie=compute\_Ie(f,ycen);

Time<<Im.real()<<" , "<<Im.imag()<<" , "<<Vm.real()<<" , "<<Vm.imag()<<" , "<<Ie.real()<<" , "<<Ie.imag()<<" , "<<Ve.real()<<" , "<<Ve.imag()<<endl;

//Im , Vm , Ie , Ve

monitor\_point pin;

f.get\_point(&pin, vec(xcen,ycen,-02.5));

cdouble E1i = pin.get\_component(Ex);

cdouble E2i = pin.get\_component(Ey);

cdouble E3i = pin.get\_component(Ez);

cdouble D1i = pin.get\_component(Dx);

cdouble D2i = pin.get\_component(Dy);

cdouble D3i = pin.get\_component(Dz);

cdouble H1i = pin.get\_component(Hx);

cdouble H2i = pin.get\_component(Hy);

cdouble H3i = pin.get\_component(Hz);

cdouble B1i = pin.get\_component(Bx);

cdouble B2i = pin.get\_component(By);

cdouble B3i = pin.get\_component(Bz);

monitor\_point po;

f.get\_point(&po, vec(xcen,ycen,02.5));

cdouble E1o = po.get\_component(Ex);

cdouble E2o = po.get\_component(Ey);

cdouble E3o = po.get\_component(Ez);

cdouble D1o = po.get\_component(Dx);

cdouble D2o = po.get\_component(Dy);

cdouble D3o = po.get\_component(Dz);

cdouble H1o = po.get\_component(Hx);

cdouble H2o = po.get\_component(Hy);

cdouble H3o = po.get\_component(Hz);

cdouble B1o = po.get\_component(Bx);

cdouble B2o = po.get\_component(By);

cdouble B3o = po.get\_component(Bz);

FieldsIn<<H1i.real() <<" , "<<H1i.imag()<<" , "<<H2i.real()<<" , "<<H2i.imag()<<" , "<<H3i.real()<<" , "<<H3i.imag()<<" , "<<B1i.real()<<" , "<<B1i.imag()<<" , "<<B2i.real()<<" , "<<B2i.imag()<<" , "<<B3i.real()<<" , "<<B3i.imag()<<" , "<<E1i.real()<<" , "<<E1i.imag()<<" , "<<E2i.real()<<" , "<<E2i.imag()<<" , "<<E3i.real()<<" , "<<E3i.imag()<<" , "<<D1i.real()<<" , "<<D1i.imag()<<" , "<<D2i.real()<<" , "<<D2i.imag()<<" , "<<D3i.real()<<" , "<<D3i.imag()<<endl;

FieldsOut<<H1o.real()<<" , "<<H1o.imag()<<" , "<<H2o.real()<<" , "<<H2o.imag()<<" , "<<H3o.real()<<" , "<<H3o.imag()<<" , "<<B1o.real()<<" , "<<B1o.imag()<<" , "<<B2o.real()<<" , "<<B2o.imag()<<" , "<<B3o.real()<<" , "<<B3o.imag()<<" , "<<E1o.real()<<" , "<<E1o.imag()<<" , "<<E2o.real()<<" , "<<E2o.imag()<<" , "<<E3o.real()<<" , "<<E3o.imag()<<" , "<<D1o.real()<<" , "<<D1o.imag()<<" , "<<D2o.real()<<" , "<<D2o.imag()<<" , "<<D3o.real()<<" , "<<D3o.imag()<<endl;

//Hx , Hy , Hz , Bx , By , Bz , Ex , Ey , Ez , Dx , Dy , Dz

}

if((i%1000)==0)

{

cout<<"End? (1/0):";

cin>>stop;

}

}

double \*fl1 = flux1.flux();

double \*fl2 = flux2.flux();

cout<<"Flux Harmonics"<<endl;

for (int i = 0; i < Nfreq; ++i) {

Fluxes<<(fmin + i \* flux1.dfreq)<<" , "<<fl1[i]<<" , "<<fl2[i]<<endl;

//freq , fluxin , fluxout

}

int num\_bands=1;

int \* bands=new int [num\_bands];

double \* vgrp=new double [num\_bands\*Nfreq];

cdouble \* coeffs=new cdouble [2\*num\_bands\*Nfreq];

bands[0]=1;

for (int i = 1; i <= Nfreq; ++i) {

vgrp[i]=0.0;

}

//f.get\_eigenmode\_coefficients(flux1,box1,bands,num\_bands,1,divisions,DEFAULT\_SUBPIXEL\_TOL,coeffs,vgrp);

cout<<"EigenModes"<<endl;

for (int i = 0; i < Nfreq; ++i) {

//cout<<(fmin + i \* flux1.dfreq)<<" , "<<bands[i]<<" , "<<coeffs[i]<<endl;

//freq , fluxin , fluxout

}

/\*void get\_eigenmode\_coefficients(dft\_flux flux, const volume &eig\_vol, int \*bands, int num\_bands,

int parity, double eig\_resolution, double eigensolver\_tol,

std::complex<double> \*coeffs, double \*vgrp,

kpoint\_func user\_kpoint\_func, void \*user\_kpoint\_data,

vec \*kpoints, vec \*kdom, direction d);

\*/

cout<<"Skin Effect"<<endl;

for (double y=-05.0;y<=05.0;y=y+00.01)

{

monitor\_point pin;

f.get\_point(&pin, vec(xcen,y,zcen));

cdouble E1i = pin.get\_component(Ex);

cdouble E2i = pin.get\_component(Ey);

cdouble E3i = pin.get\_component(Ez);

cdouble D1i = pin.get\_component(Dx);

cdouble D2i = pin.get\_component(Dy);

cdouble D3i = pin.get\_component(Dz);

cdouble H1i = pin.get\_component(Hx);

cdouble H2i = pin.get\_component(Hy);

cdouble H3i = pin.get\_component(Hz);

cdouble B1i = pin.get\_component(Bx);

cdouble B2i = pin.get\_component(By);

cdouble B3i = pin.get\_component(Bz);

Skin<<H1i.real() <<" , "<<H1i.imag()<<" , "<<H2i.real()<<" , "<<H2i.imag()<<" , "<<H3i.real()<<" , "<<H3i.imag()<<" , "<<B1i.real()<<" , "<<B1i.imag()<<" , "<<B2i.real()<<" , "<<B2i.imag()<<" , "<<B3i.real()<<" , "<<B3i.imag()<<" , "<<E1i.real()<<" , "<<E1i.imag()<<" , "<<E2i.real()<<" , "<<E2i.imag()<<" , "<<E3i.real()<<" , "<<E3i.imag()<<" , "<<D1i.real()<<" , "<<D1i.imag()<<" , "<<D2i.real()<<" , "<<D2i.imag()<<" , "<<D3i.real()<<" , "<<D3i.imag()<<endl;

}

cout<<"SpaceEvolution"<<endl;

//for (double y=(ycen-dymin);y<=(ycen+dymin);y=y+0.001)

for (double z=-05.0;z<=05.0;z=z+00.1)

{

cdouble Im=compute\_Im(f,z);

cdouble Ie=compute\_Ie(f,z);

cdouble Vm=compute\_Vm(f,z);

cdouble Ve=compute\_Ve(f,z);

Space <<Im.real()<<" , "<<Im.imag()<<" , "<<Vm.real()<<" , "<<Vm.imag()<<" , "<<Ie.real()<<" , "<<Ie.imag()<<" , "<<Ve.real()<<" , "<<Ve.imag()<<endl;

//Im , Vm , Ie , Ve

}

Time.close();

Space.close();

FieldsIn.close();

FieldsOut.close();

Fluxes.close();

return 0;

}

## MATLAB Codes

## Plotting Magnetic Susceptibility and Hysteresis Loop for Ferromagnetic material

clc;clear all;

max=2000;

MMF(1:max+1)=(0:max)-(max/2);

ind=1;

for ind=1:max+1

chip(ind)=10000\*exp(-(abs(MMF(ind)-500))\*(abs(MMF(ind)-500))/50000);

chin(ind)=-10000\*exp(-(abs(MMF(ind)+500))\*(abs(MMF(ind)+500))/50000);

end

% hold on;

% plot((-max/2):1:(max/2),chip)

% plot((-max/2):1:(max/2),chin,'r')

% grid on;

% xlabel('H (A/m)');

% ylabel('Magnetic Susceptibility \chi\_m');

% legend('\chi\_m^+','\chi\_m^-')

B(1)=2.5;

Hmax=1000;

Happ=[Hmax:-1:(-Hmax) (-Hmax):1:(Hmax)];

hold on;

for ind=2:length(Happ)

if (Happ(ind)>Happ(ind-1))

munet=(chip(Happ(ind)+(Hmax+1))+1);

dB=(Happ(ind)-Happ(ind-1))\*munet\*(4\*pi\*1e-7);

else

munet=(chin(Happ(ind)+(Hmax+1))+1);

dB=(-Happ(ind)+Happ(ind-1))\*munet\*(4\*pi\*1e-7);

end

B(ind)=B(ind-1)+dB;

end

% plot(Happ,B);

% grid('on');

% xlabel('H (A/m)');

% ylabel('B (T)');

## Evolution of Magnetic displacement current and Voltage for Magnetic Transmission Line

clc;clear all;

f=fopen('TimeEvolution.txt');

l=fgetl(f);

i=1;

while ischar(l)

%%disp(l);

text{i}=l;

data{i}=sscanf(text{i},'%f , %f , %f , %f , %f , %f , %f , %f');

A1(i)=data{i}(1);

A2(i)=data{i}(2);

A3(i)=data{i}(3);

A4(i)=data{i}(4);

A5(i)=data{i}(5);

A6(i)=data{i}(6);

A7(i)=data{i}(7);

A8(i)=data{i}(8);

l=fgetl(f);

i=i+1;

end

epsr=0.9999;

a0=1e-4;%0.1mm

c0=2.99792458e8;%Speed of Light (m/s)

f0=c0/a0;%3000GHz

t0=1/f0;%0.33e-12 (s)

mu0=4\*pi\*(1e-7);% (H/m)

eps0=8.854187817e-12;% (F/m)

I0=1; %(A)

E0=I0/(a0\*eps0\*c0);%Electric Field

D0=I0/(a0\*c0);%Electric Displacement Field

B0=I0/(a0\*eps0\*c0\*c0);%Magnetic Field

H0=I0/(a0);%Magnetizing Field

V0=I0/(eps0\*c0);%Electric Field

hold on;

A1=A1\*V0;A2=A2\*V0;

A3=A3\*I0;A4=A4\*I0;

A5=A5\*I0;A6=A6\*I0;

A7=A7\*V0;A8=A8\*V0;

t=100\*t0\*(1:length(A1));

subplot(2,1,1)

hold on;plot(t,A1);plot(t,A2,'r');%Im

ylabel('Magnetic Current (V)');

xlabel('Time');

legend('Re','Im');

subplot(2,1,2)

hold on;plot(t,A3);plot(t,A4,'r');%Vm

ylabel('Magnetic Voltage (A)');

xlabel('Time');

legend('Re','Im');

## Calculation of Intrinsic Impedance, Propagation Constant, per unit length Conductance, per unit length Reluctance and per unit length Susceptance for Magnetic Transmission Line

## 

clc;clear all;

%hold on;

%%

f=fopen('F1.txt');

File=1;

l=fgetl(f);

in=1;

Prev=1600\*(File-1);

while ischar(l)

%for kj=1:81

%%disp(l);

text{in}=l;

data{in}=sscanf(text{in},'%f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f , %f');

Hx(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(3)+1i\*data{in}(4);

Hy(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(5)+1i\*data{in}(6);

Hz(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(7)+1i\*data{in}(8);

Bx(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(9)+1i\*data{in}(10);

By(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(11)+1i\*data{in}(12);

Bz(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(13)+1i\*data{in}(14);

Ex(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(15)+1i\*data{in}(16);

Ey(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(17)+1i\*data{in}(18);

Ez(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(19)+1i\*data{in}(20);

Dx(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(21)+1i\*data{in}(22);

Dy(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(23)+1i\*data{in}(24);

Dz(data{in}(1)-Prev,(((data{in}(2)+10)\*4)+1))=data{in}(25)+1i\*data{in}(26);

l=fgetl(f);

in=in+1;

end

epsr=10;

a0=1e-4;%0.1mm

c0=2.99792458e8;%Speed of Light (m/s)

f0=c0/a0;%3000GHz

t0=1/f0;%0.33e-12 (s)

mu0=4\*pi\*(1e-7);% (H/m)

eps0=8.854187817e-12;% (F/m)

I0=1; %(A)

E0=I0/(a0\*eps0\*c0);%Electric Field

D0=I0/(a0\*c0);%Electric Displacement Field

B0=I0/(a0\*eps0\*c0\*c0);%Magnetic Field

H0=I0/(a0);%Magnetizing Field

sigmaD0=(epsr\*eps0\*c0)/a0;

hold on;

subplot(4,1,1)

hold on;

T=t0;

Fs=1/T;

L=45;

L=2^nextpow2(L);

% NFFT=2^nextpow2(L);

% FHxi=(fft(Hx(1:L,5)\*H0,NFFT)/L)();

% FHxi(2:end-1)=

% f=Fs/2\*linspace(0,1,NFFT/2+1);

FHxi=(fft(Hx(1:L,2)\*H0,L));

FHxi=FHxi(1:L/2+1);

%FHxi(2:end-1)=2\*FHxi(2:end-1)

f=Fs\*(0:L/2+1);

f=f';

FHxo=(fft(Hx(1:L,12)\*H0,L));

FHxo=FHxo(1:L/2+1);

%FHxo(2:end-1)=2\*FHxo(2:end-1);

Gamma=log(FHxo./FHxi)/(-(10/80)\*(2e-3));

subplot(3,1,1)

hold on;%plot(mag3(mag(A13,A14),mag(A15,A16),mag(A17,A18)));%E

plot(f(2:L/2+1),real(Gamma(2:L/2+1)));

xlabel('Frequency (Hz)')

ylabel('\alpha (Np.m^-^1)');

axis([0 5e11 1.32e5 1.38e5])

subplot(3,1,2)

plot(f(2:L/2+1),abs(imag(Gamma(2:L/2+1))));

ylabel('\beta (rad.m^-^1)');

xlabel('Frequency (Hz)')

axis([0 5e11 1e4 1.3e4])

subplot(3,1,3)

plot(f(2:L/2+1),f(2:L/2+1)./abs(imag(Gamma(2:L/2+1))));

ylabel('vp (m.s^-^1)');

xlabel('Frequency (Hz)')

axis([0 5e11 0 5e7])

% X = 1/(4\*sqrt(2\*pi\*0.01))\*(exp(-t.^2/(2\*0.01)));

T=t0;

Fs=1/T;

L=45;

NFFT=2^nextpow2(L);

FEx=fft(Ex(1:L,2)\*E0,NFFT)/L;

f=Fs/2\*linspace(0,1,NFFT/2+1);

FHx=fft(Hx(1:L,2)\*H0,NFFT)/L;

f=Fs/2\*linspace(0,1,NFFT/2+1);

Z=FEx./FHx;

subplot(2,1,1)

hold on;%plot(mag3(mag(A13,A14),mag(A15,A16),mag(A17,A18)));%E

plot(f(2:NFFT/2+1),2\*abs(Z(2:NFFT/2+1)));

xlabel('Frequency (Hz)')

ylabel('|Z\_w (Ohm)|');

axis([0 5e11 3.3e4 3.45e4])

subplot(2,1,2)

plot(f(2:NFFT/2+1),angle(Z(2:NFFT/2+1))\*(180/pi));

ylabel('\Theta Z\_w (deg)');

xlabel('Frequency (Hz)');

axis([0 5e11 170 190])

XLm=(imag(Gamma(1:NFFT/2+1).\*Z(1:NFFT/2+1)));

Gm=(real(Gamma(1:NFFT/2+1)./Z(1:NFFT/2+1)));

Rm=(Gm')\*(-1).\*(2\*pi\*f);%Reluctance

XCm=(imag(Gamma(1:NFFT/2+1)./Z(1:NFFT/2+1)));

subplot(4,1,1);

plot(f,(XLm(1:NFFT/2+1)));

ylabel('XLm(H/m)');

xlabel('Frequency (Hz)');

%axis([0 1e11 -5e9 5e9])

subplot(3,1,1);

plot(f(2:NFFT/2+1),(Gm(2:NFFT/2+1)));

ylabel('Conductance GL (S/m)');

xlabel('Frequency (Hz)');

axis([0 5e11 -8.5 -7.5])

subplot(3,1,2);

plot(f(2:NFFT/2+1),(Rm(2:NFFT/2+1)));

ylabel('Reluctance Rmskin (1/H.m)');

xlabel('Frequency (Hz)');

axis([0 5e11 0 3e13])

subplot(3,1,3);

plot(f(2:NFFT/2+1),(XCm(2:NFFT/2+1)));

ylabel('Susceptance XCL (S/m)');

xlabel('Frequency (Hz)');

axis([0 5e11 0 1])

## Plotting Wideband Transformer Bandwidth calculated using Fourier Transform of Poynting Fluxes

clc;clear all;

f=fopen('Flux.txt');

l=fgetl(f);

i=1;

while ischar(l)

%%disp(l);

text{i}=l;

data{i}=sscanf(text{i},'%f , %f , %f');

A1(i)=data{i}(1);

A2(i)=data{i}(2);

A3(i)=data{i}(3);

l=fgetl(f);

i=i+1;

end

epsr=0.9999;

a0=1e-4;%0.1mm

c0=2.99792458e8;%Speed of Light (m/s)

f0=c0/a0;%3000GHz

t0=1/f0;%0.33e-12 (s)

mu0=4\*pi\*(1e-7);% (H/m)

eps0=8.854187817e-12;% (F/m)

I0=1; %(A)

E0=I0/(a0\*eps0\*c0);%Electric Field

D0=I0/(a0\*c0);%Electric Displacement Field

B0=I0/(a0\*eps0\*c0\*c0);%Magnetic Field

H0=I0/(a0);%Magnetizing Field

S0=(I0\*I0)/(eps0\*c0\*a0\*a0);%//Poynting Vector

sigmaD0=(epsr\*eps0\*c0)/a0;%Electric Conductivity

hold on;

subplot(3,1,1)

plot(A1\*f0,abs(-A2\*S0));

axis([0 4e9 S0\*0.01 S0\*40]);

ylabel('|Sin| (W/m^2)');

xlabel('frequency (Hz)');

subplot(3,1,2)

plot(A1\*f0,abs(-A3\*S0));

axis([0 4e9 S0\*0.01 S0\*25]);

ylabel('|Sout| (W/m^2)');

xlabel('frequency (Hz)');

subplot(3,1,3)

C=log(A2./A3);

C=C(1:5:1000);

A1=A1(1:5:1000);

plot((f0\*A1),(abs(C)));

axis([0 4e9 -1 5]);

ylabel('Insertion Loss');

xlabel('frequency (Hz)');